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Manifestation of exciton-exciton interaction in scintillator response

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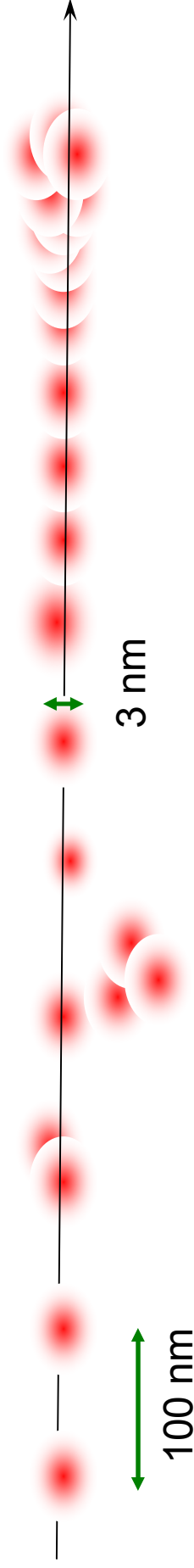
Outline

- Exciton-exciton interaction under XUV/X ray/ γ ray excitation: difficulties of characterization
- Experiments with high-density UV/VUV excitation
- Methods of data treatment
- Conclusions

Scintillator nonproportional response

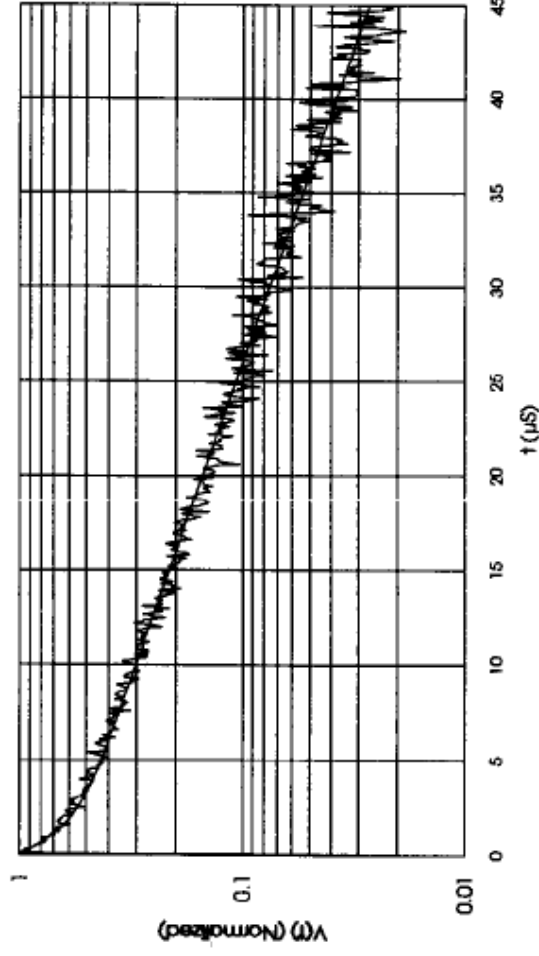
- Excitation density effects:
Vasil'ev, IEEE Trans. Nucl. Sci. 55 (2008) 1054
- Luminescence excitation in the fundamental absorption region is intrinsically non-linear process
- Luminescence non-linearity is displayed in decay kinetics
- Luminescence yield depends on the density of initially created excitations, resulting in non-proportionality
- **Reason:** Initial electron track structure is defined by isolated and overlapped clusters of excitations with initial size of about 3 nm

↑ Luminescence quenching mechanisms involved
Method: comparison UV vs XUV/X rays



Decay kinetics of CdWO₄ excitonic emission under different excitations

- 0.8 μS Gillette, 1950. Rev. Sci. Instrum. 21, p. 294 (γ rays)
- 1.1 μS , 14.5 μS Kinloch et al., IEEE Trans. Nucl. Sci. 41, 752 (1994) (γ rays)
- 2 μS , 15 μS Deych et al., Proc. SCINT95, 1996, p. 36 (γ rays)
- 5 μS , 20 μS Melcher et al., IEEE Trans. Nucl. Sci. 36, 1188 (1989) (X rays)
- 7.8 μS Beard et al., 1962. J Appl. Phys.. 33, p. 144 (α particles)
- 9 μS Grabmaier. IEEE Trans. Nucl. Sci. 31, 372 (1984) (X rays)
- 13-15 μS under optical excitation! Many papers. (UV photons)



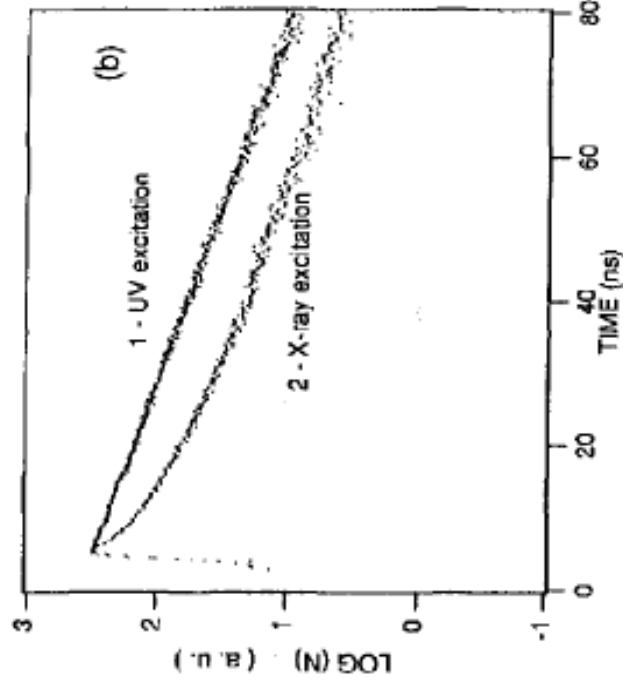
Kinloch et al., IEEE Trans. Nucl. Sci. 41, 752 (1994)

10 microcurie Cs-137 source:
662 keV γ photons

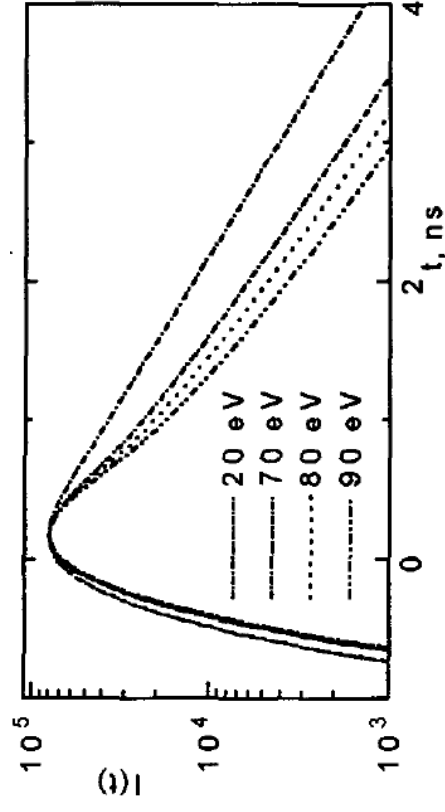
Emission decay curves under XUV and X-ray excitation



Pedrini, et al., Chem. Phys. Lett. 206 (1993) 470



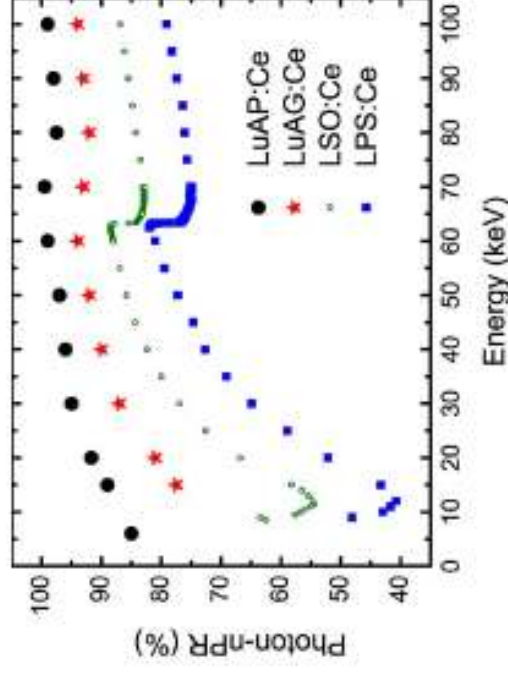
Belsky at al., J. Electr. Spectrosc. Rel. Phen. 79 (1996) 147



Crossluminescence(!?)

Difficulties with high-energy excitation

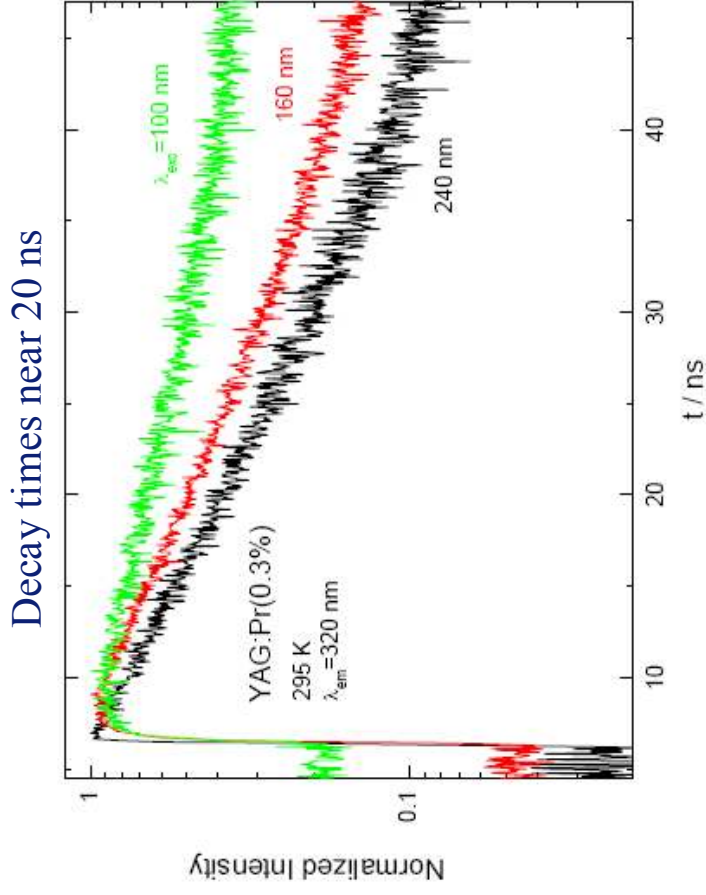
- Complex relaxation processes
- Radiation damage, colour defect creation
- Difficult to estimate number of excitations created per radiation photon
- Energy transfer from the host to a luminescence centre → additional slow components in emission decay
- Interaction of luminescence centre with transient defects → possible shortening of emission decay kinetics



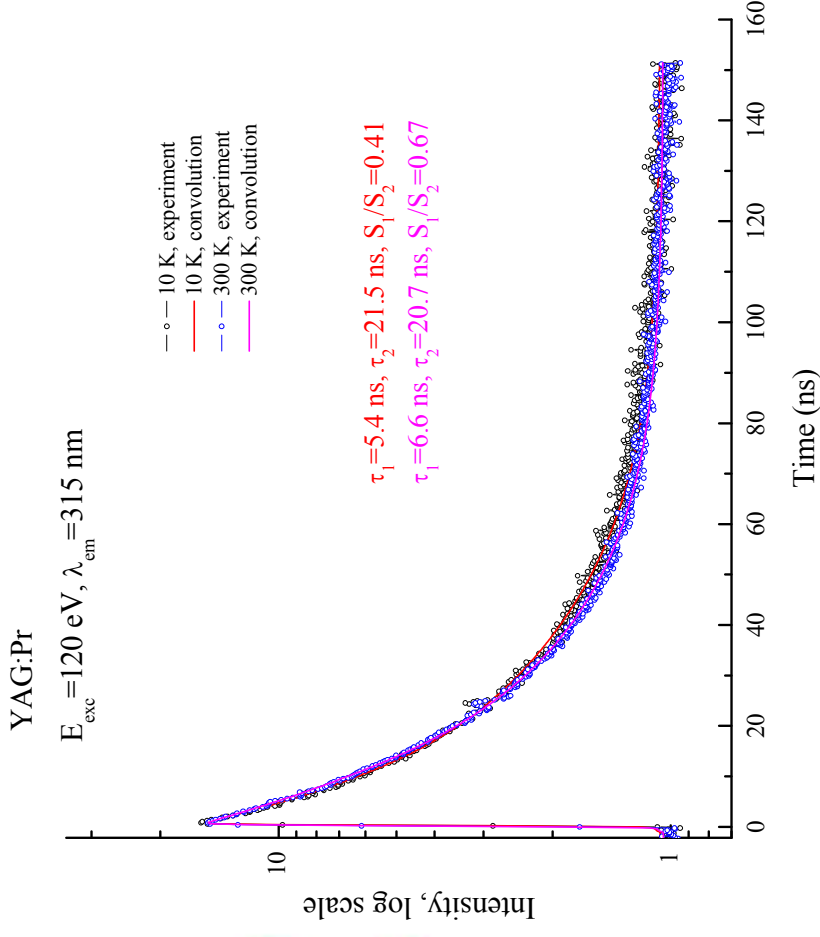
Khodyuk&Dorenbos, IEEE Trans. Nucl. Sci. 59 (2012) 3320

Interaction with transient defects: YAG:Pr³⁺

Intrinsic f-d or low-energy excitation



High-energy XUV excitation



How to distinguish those changes in luminescence yield and decay kinetics under high-energy excitation, which are due to high excitation density? Experiments in better controlled conditions.

Experiments performed

- High-order harmonics generation (HHG): **23-32 eV, 10-15 fs**
- Free electron laser (FEL): **89 eV, 25 fs**
- Optical parametric amplifier (OPA, 240 - 2600 nm, 1-200 $\mu\text{J}/\text{pulse}$, **100 fs, 1 kHz** \rightarrow We worked at **3.9 – 5.2 eV**)
- 3rd harmonic of a Ti-sapphire laser, **4.66 eV, 80 fs**

Advantage: 1) laser \rightarrow measurable pulse shape;
2) fs pulse \rightarrow almost no heating

Crystals studied

- Crystals with excitonic emission
CdWO₄, ZnWO₄, CaWO₄, SrWO₄, PbWO₄, CeF₃, BaF₂
- Doped crystals with excitonic and impurity emission
YAG:Ce, LuAG:Ce, LuAG:Pr, LiCAF:Eu

Theory: dipole-dipole energy transfer

• Exciton concentration:
$$\frac{\partial n(\mathbf{r}, t)}{\partial t} = -\frac{n(\mathbf{r}, t)}{\tau_r} - \gamma_{d-d}(t, \mathbf{r})n^2(\mathbf{r}, t)$$

• Dipole-dipole energy transfer rate:
$$\sim \frac{1}{\tau_r} (R_{d-d} / R)^6$$

• Dipole-dipole transfer radius:
$$R_{d-d}^6 \propto \int \omega^{-4} F_{em}(\omega) F_{exc}(\omega) d\omega$$

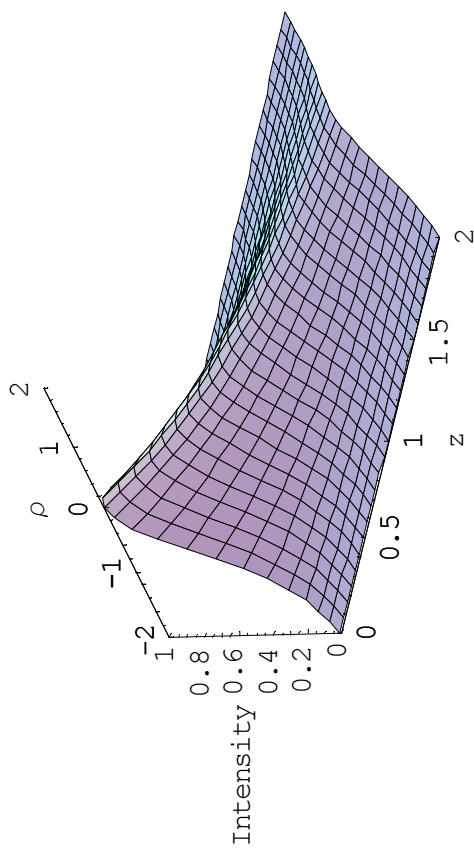
$$I(t) = \frac{\sigma I_0 e^{-t/\tau}}{\tau} \frac{-Li_2\left(-\frac{2}{3}\pi^2 R_{d-d}^3 N_{\max} \operatorname{erf}\left(\sqrt{t\tau^{-1}}\right)\right)}{\frac{2}{3}\pi^2 R_{d-d}^3 N_{\max} \operatorname{erf}\left(\sqrt{t\tau^{-1}}\right)} \quad N_{\max} \equiv I_0 \frac{\sigma\alpha}{\pi a^2}$$

I_0 – number of photons in a pulse

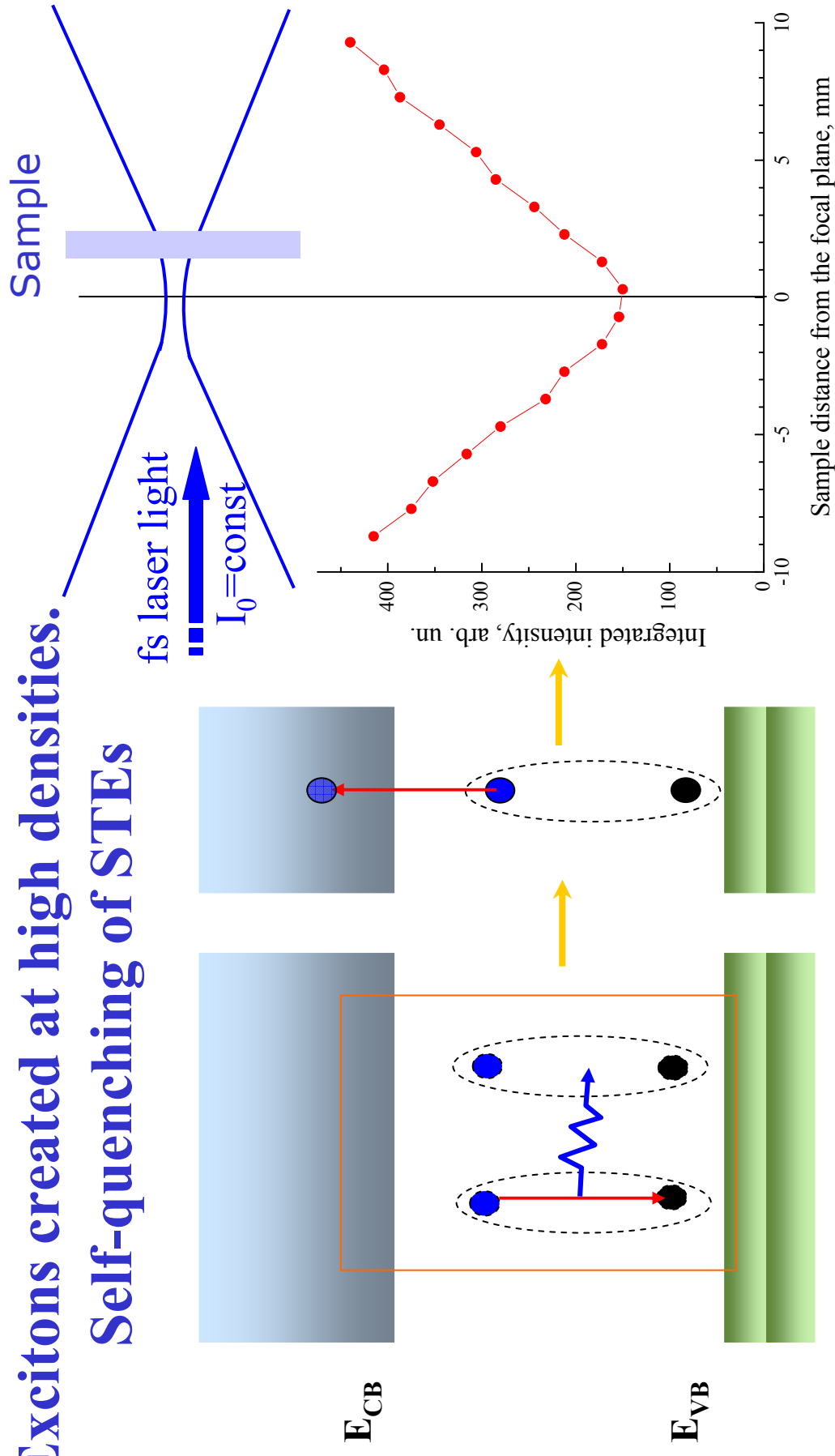
α – absorption coefficient

σ – exciton yield

a – pulse radius



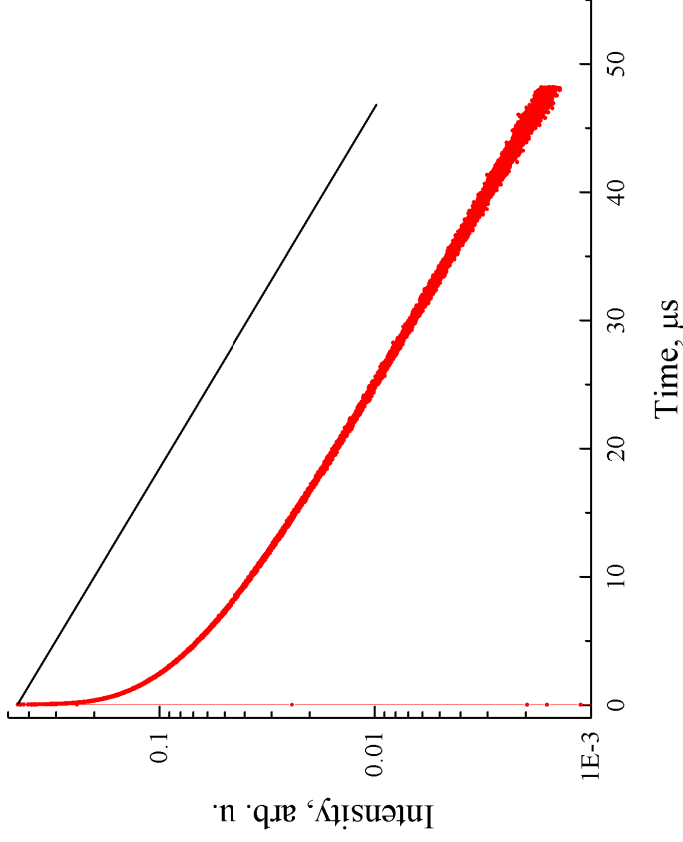
Excitons created at high densities. Self-quenching of STEs



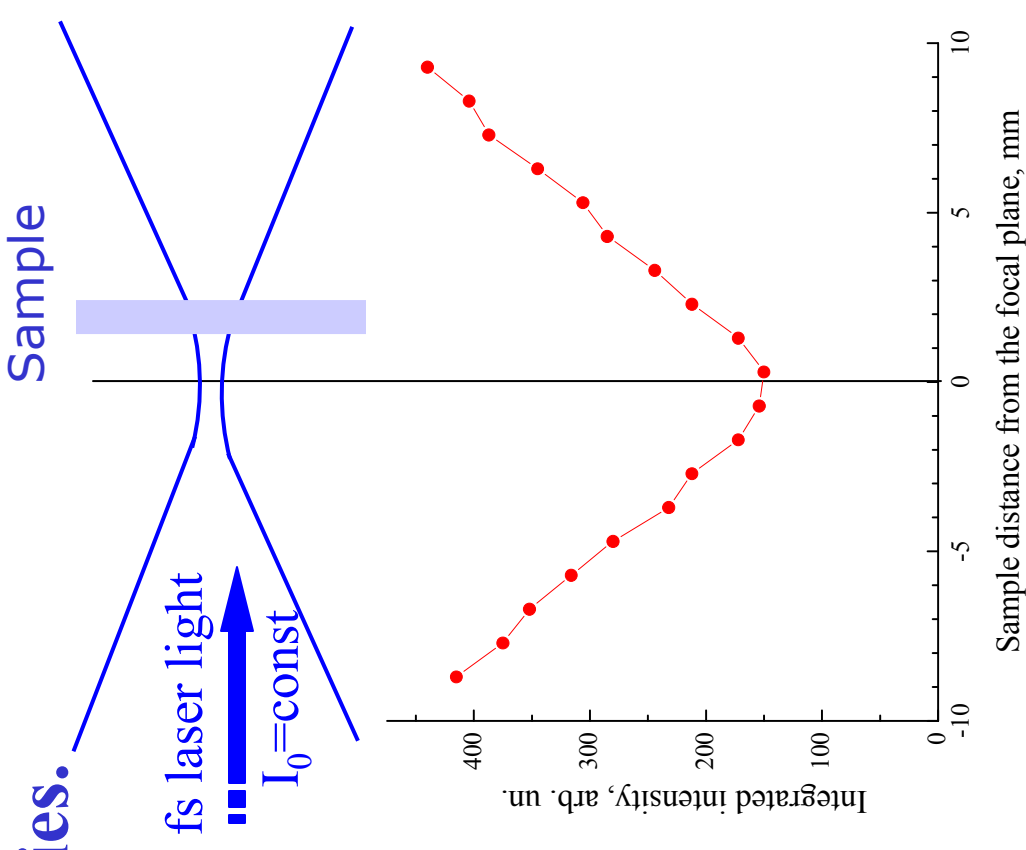
CaWO_4 , $E_{\text{exc}} = 5 \text{ eV}$ (247.5 nm), 80 fs pulse,
1 μJ pulse energy, 70 μm beam waist

Excitons created at high densities.

Self-quenching of STEs



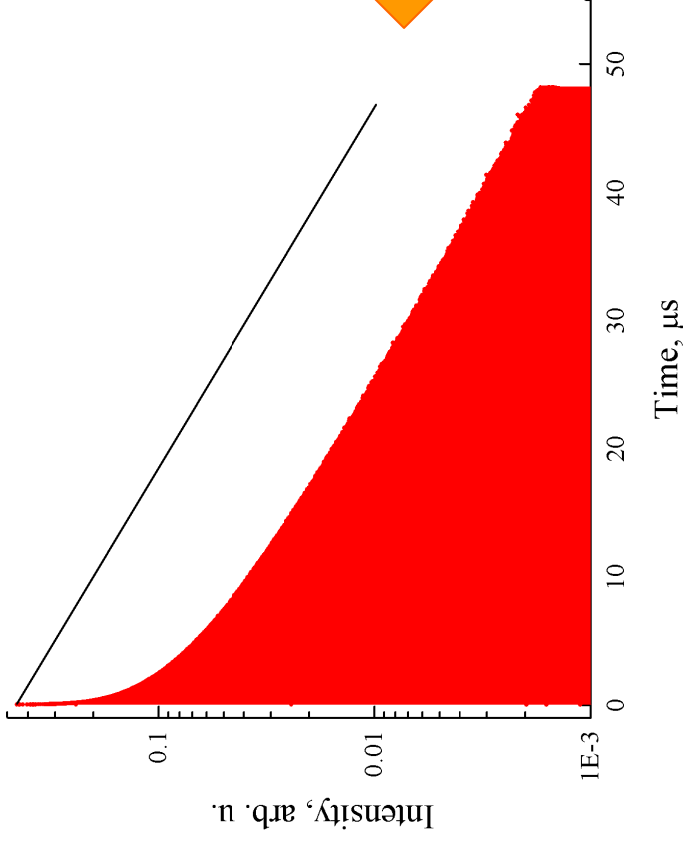
**CdWO₄, $E_{\text{exc}}=4.84$ eV (256.4 nm),
80 fs pulse, 0.6 μJ pulse energy,
130 μm beam waist**



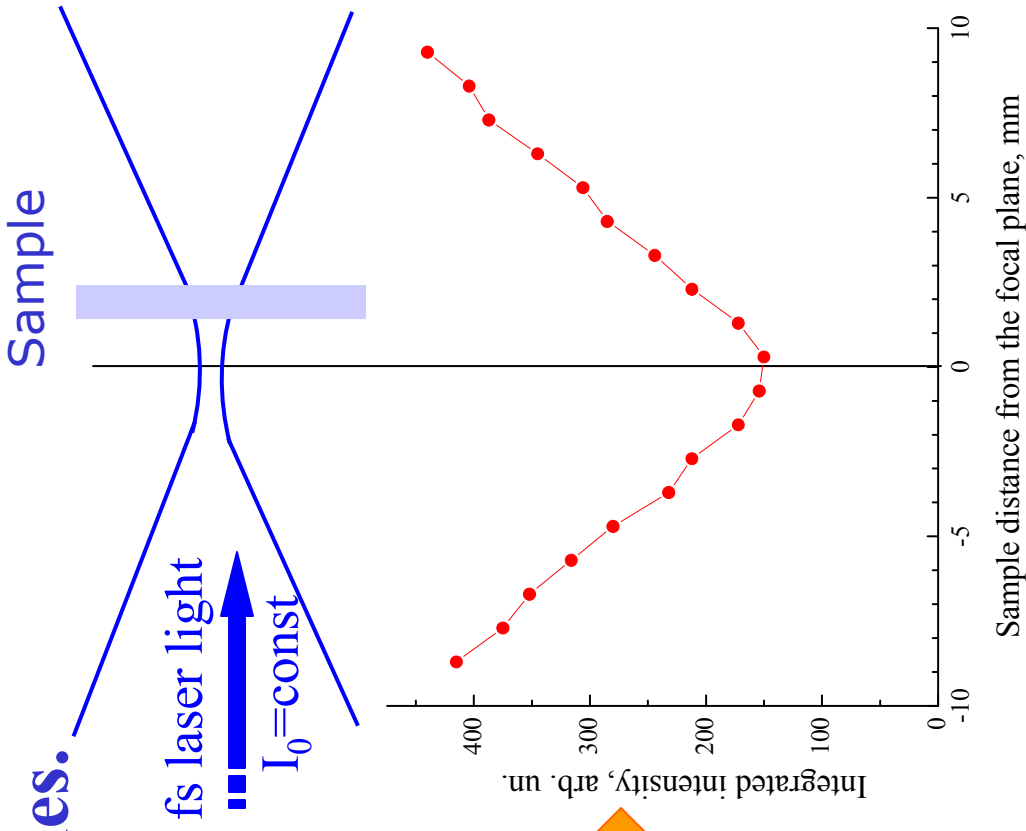
**CaWO₄, $E_{\text{exc}}=5$ eV (247.5 nm), 80 fs pulse,
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Excitons created at high densities.

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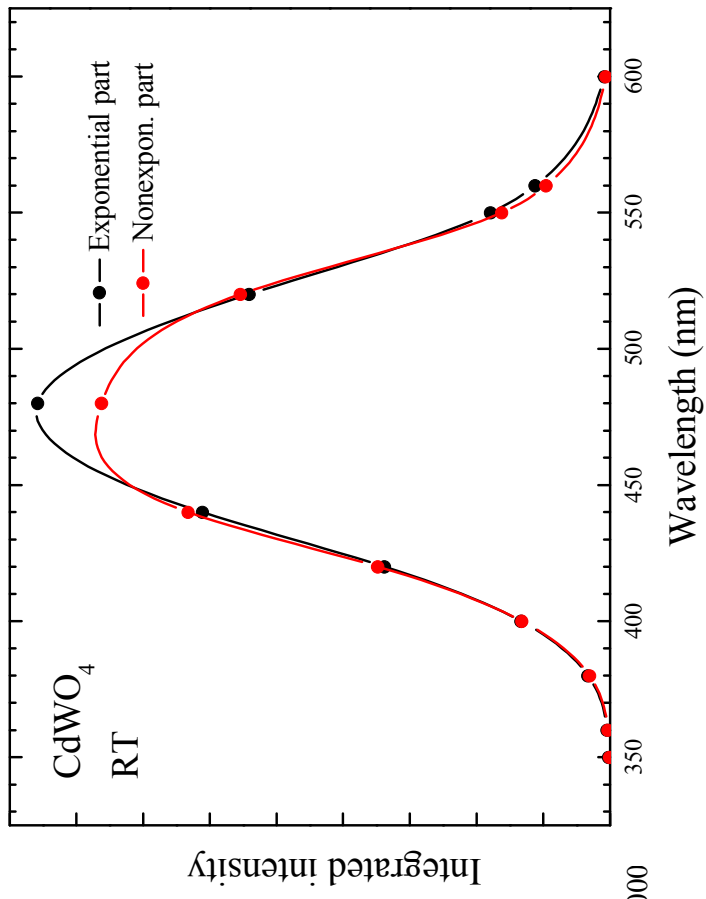
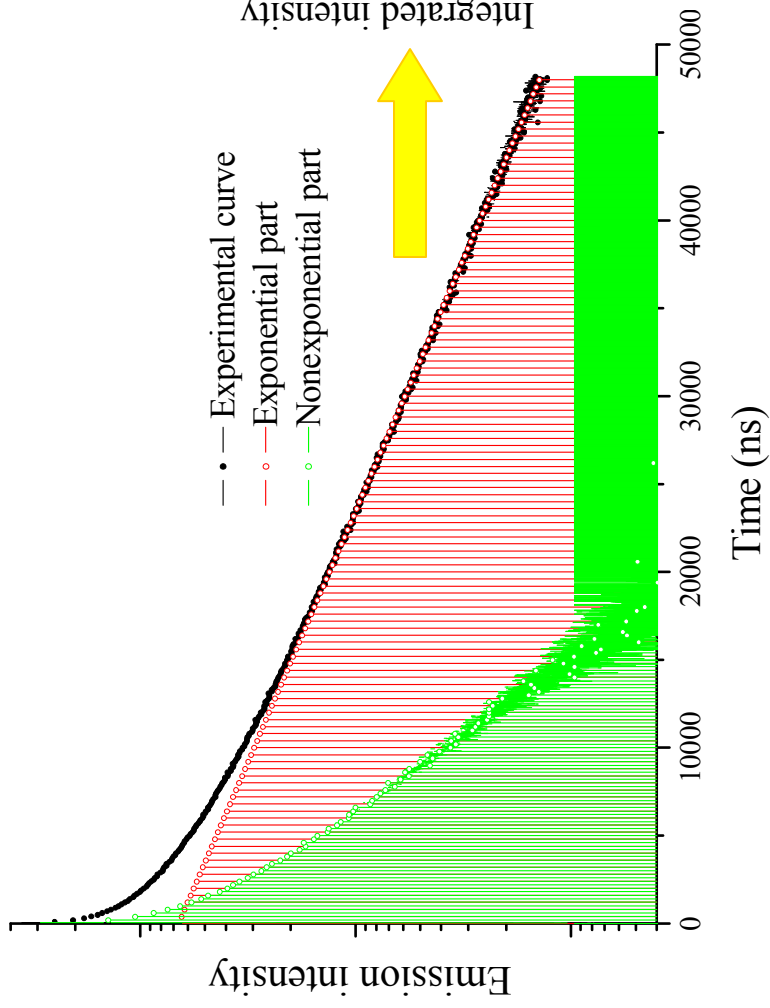


**CdWO₄, $E_{\text{exc}}=4.84$ eV (256.4 nm),
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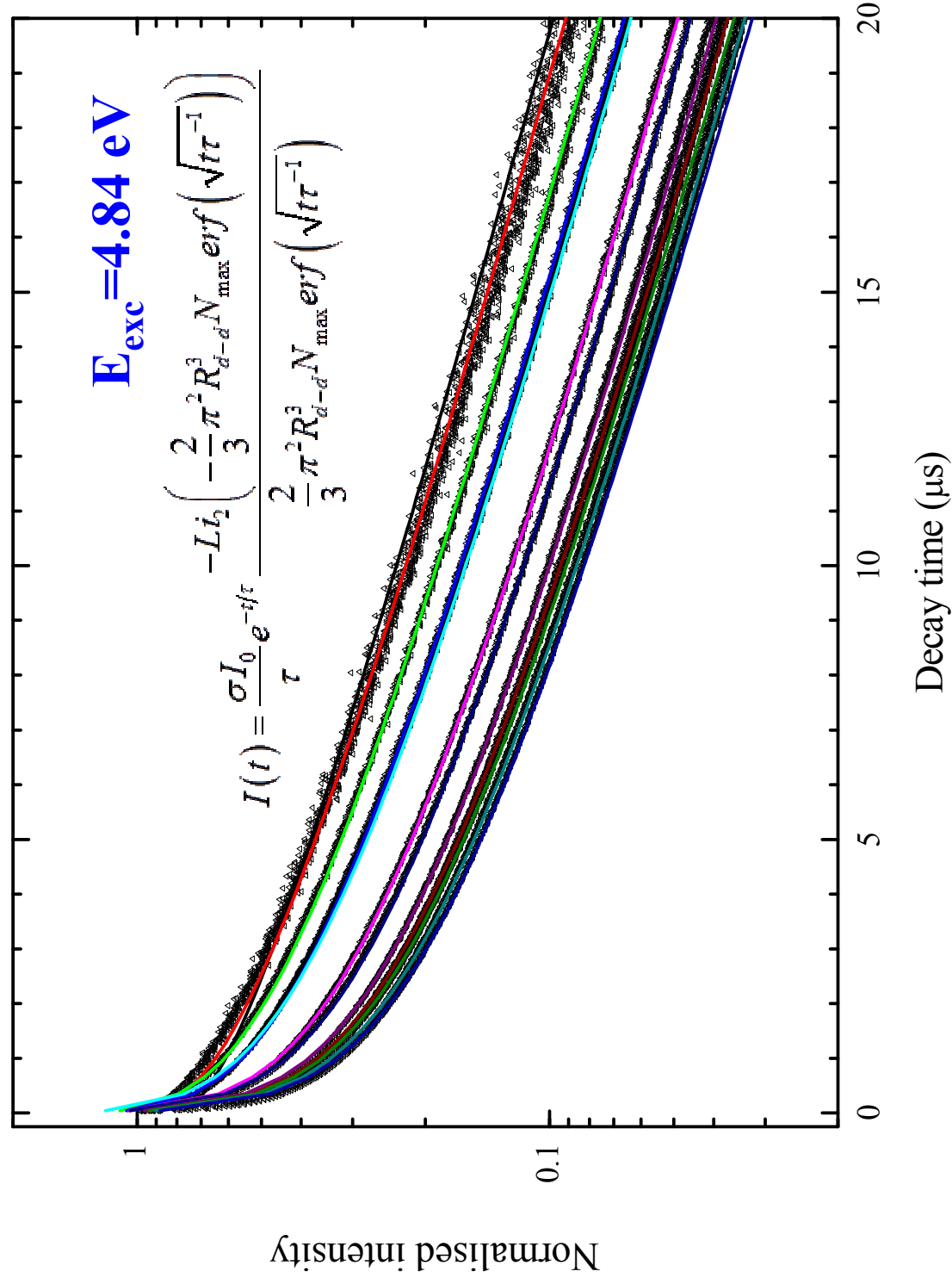
**CaWO₄, $E_{\text{exc}}=5$ eV (247.5 nm), 80 fs pulse,
1 μJ pulse energy, 70 μm beam waist**

The origin of nonexponential part



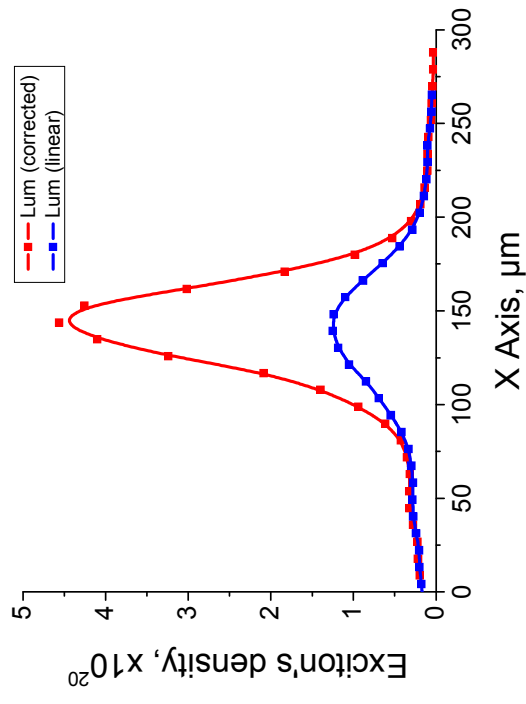
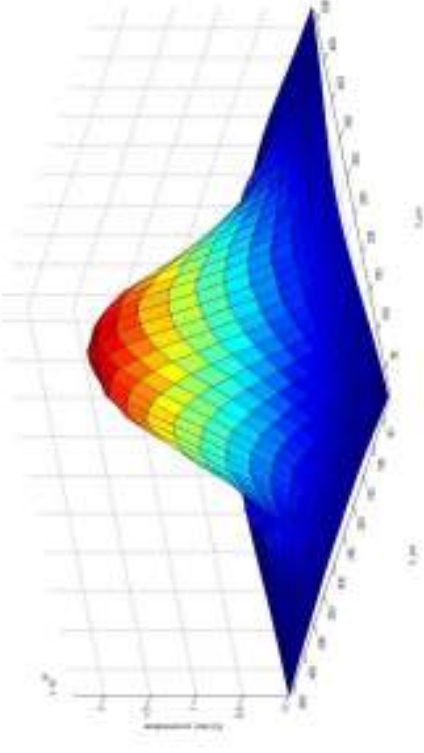
Radiative decay of **relaxed** Frenkel excitons

Fitted curves for the excitonic emission of CdWO₄

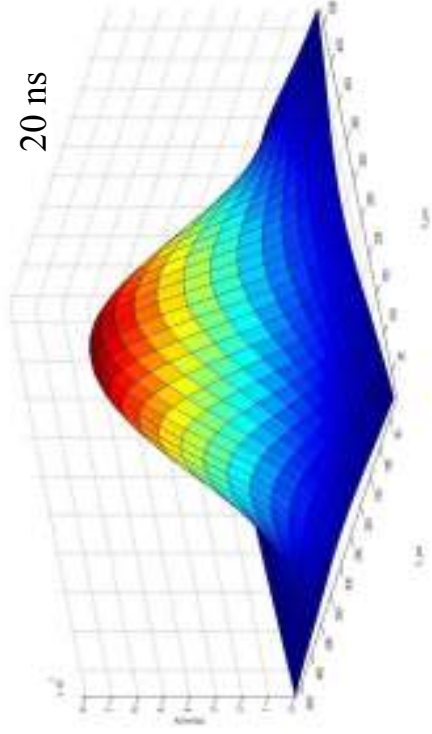


Time-resolved images with i-CCD camera

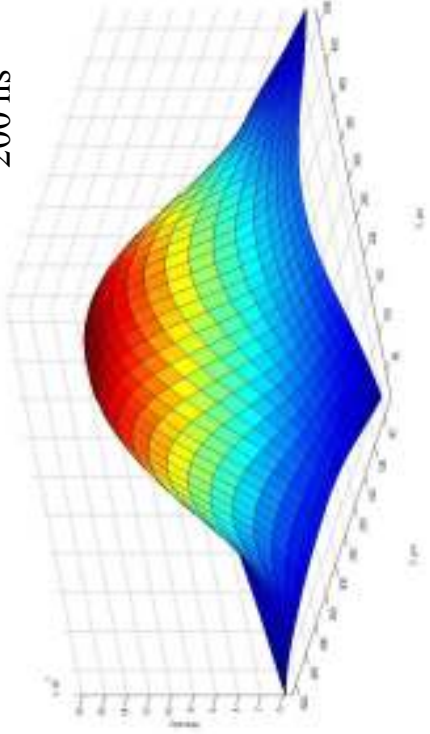
Initial distribution of excitons
(exciting beam profile)



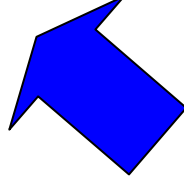
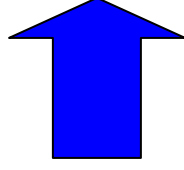
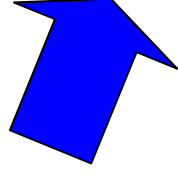
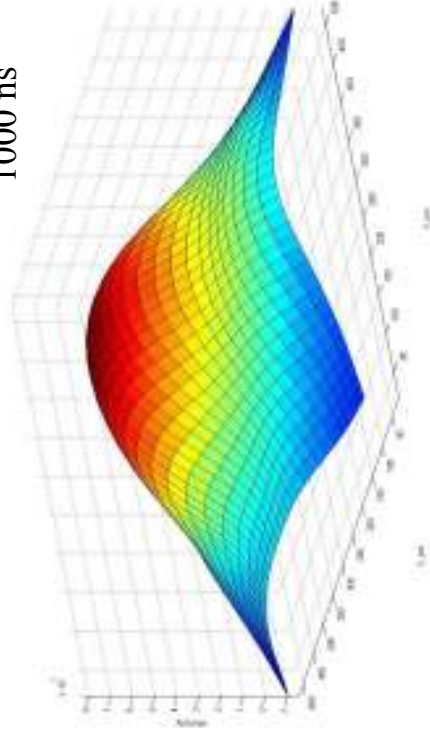
20 ns



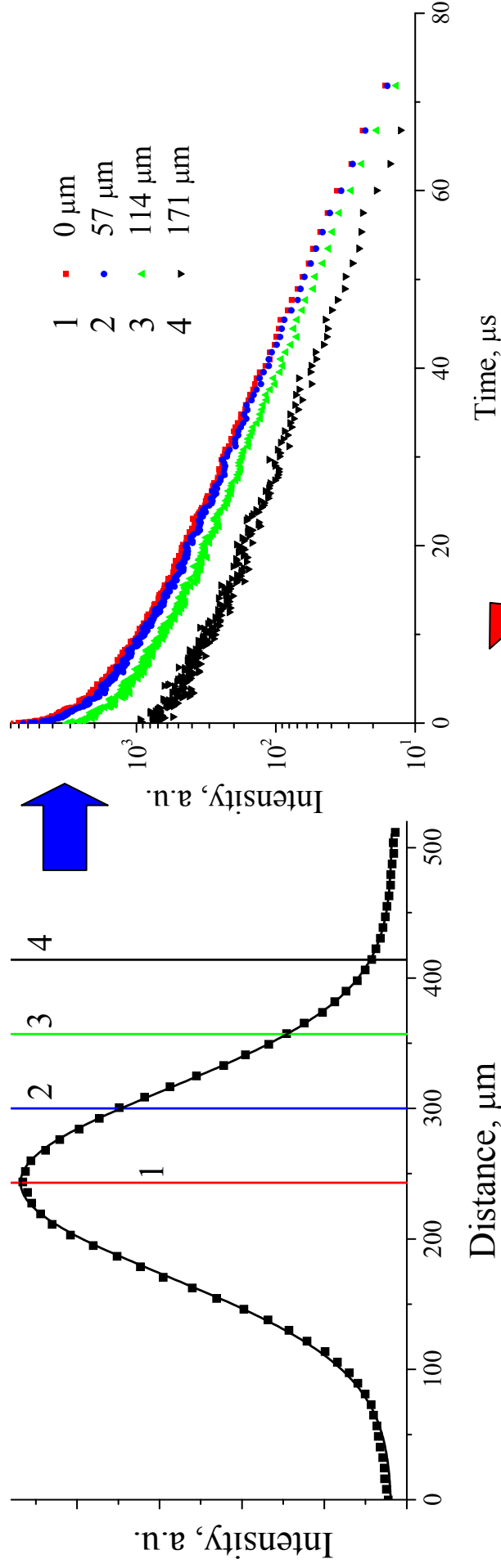
200 ns



1000 ns



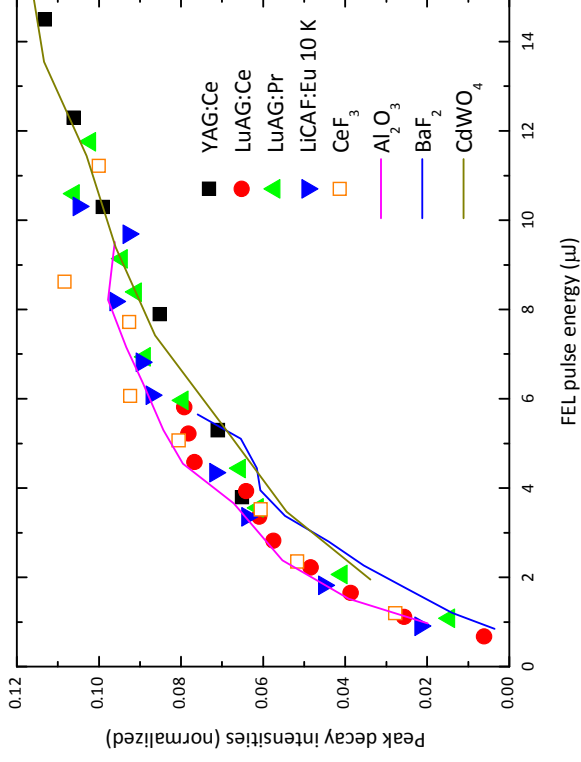
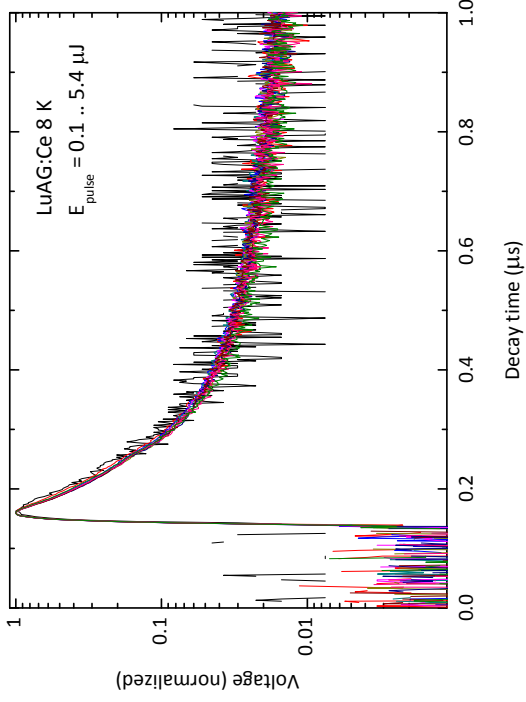
CdWO₄ emission decay kinetics at different laser spot points



$$I(\rho, t) = \frac{\Delta S}{\tau \alpha} e^{-t/\tau} \times \frac{\ln \left[1 + \frac{2}{3} \pi^2 I_0 \frac{\sigma \alpha}{\pi \alpha^2} e^{-\rho^2/\alpha^2} R_{d-d}^3 \operatorname{erf} \left(\sqrt{t/\tau} \right) \right]}{\frac{2}{3} \pi^2 R_{d-d}^3 \operatorname{erf} \left(\sqrt{t/\tau} \right)},$$

RE activated scintillators

LuAG:Ce



- No changes in the shape of decay curves with pulse power – unlike intrinsic scintillators.
(Similar observation in CsI:Tl, NaI:Tl -- Williams et al., phys. stat. sol. (b) 248 (2011) 426)
- Non-proportionality in luminescence yield:
 - almost not related to dopant concentration
 - starts well below activator saturation ($n_{\text{exc}} \ll n_{RE}$).
- **Model: quenching occurs in the precursor stage of activator luminescence.**

Empirical approach: from exciton-exciton interaction to activator luminescence quenching

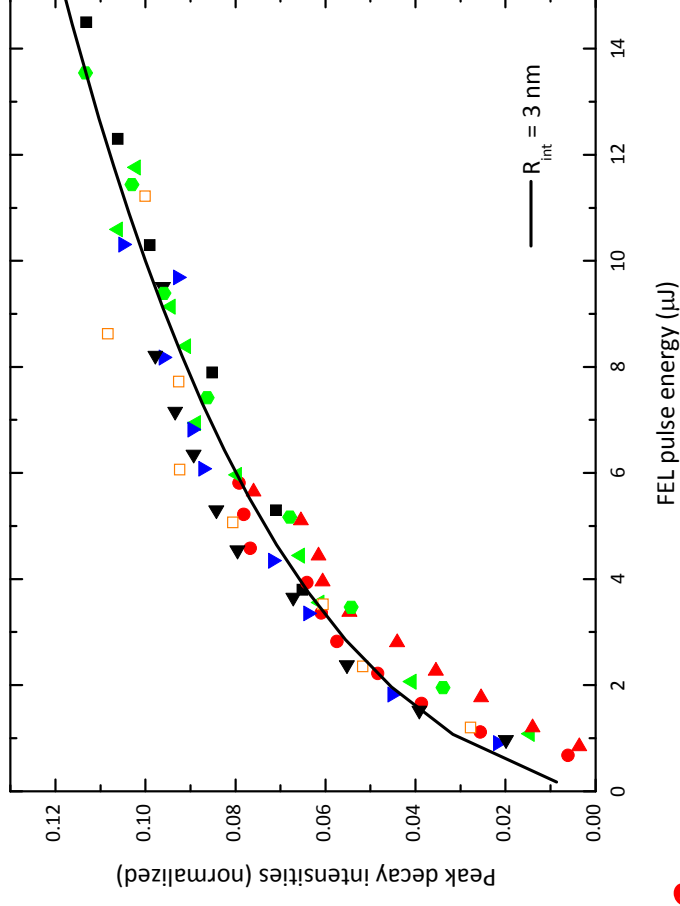
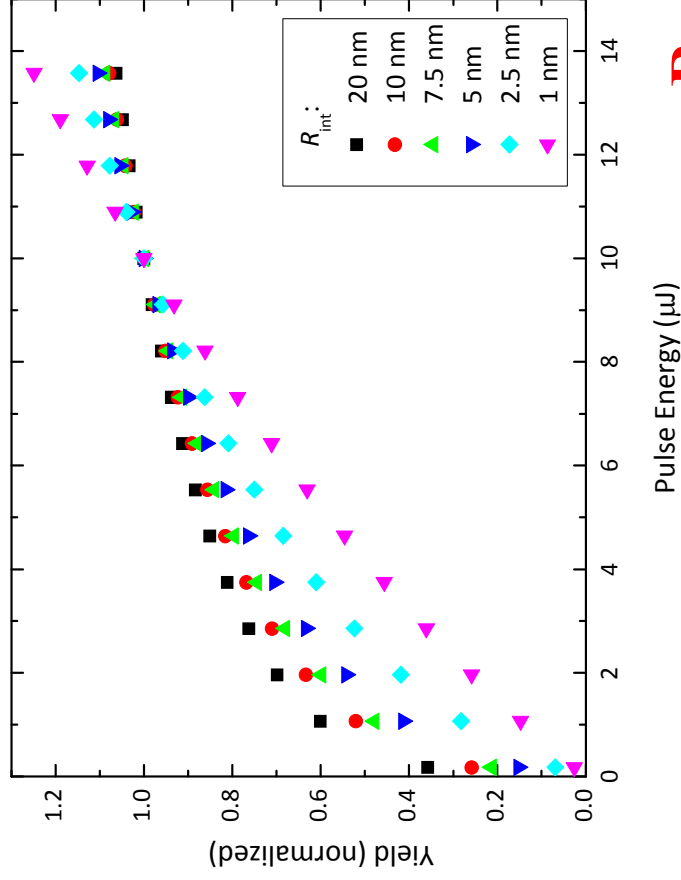
- Most simple scenario:
 - dipole-dipole interaction analog to intrinsic crystals with R_{int} ,
 - energy transfer to activator with constant rate (τ_{int}):

$$\frac{\partial n_{\text{int}}(\mathbf{r}, t)}{\partial t} = -\frac{n_{\text{int}}(\mathbf{r}, t)}{\tau_{\text{int}}} - \frac{1}{2} \gamma_{\text{int}}(t, \mathbf{r}) n_{\text{int}}^2(\mathbf{r}, t)$$

- Rate equation is equivalent to intrinsic case, luminescence yield can be calculated as

$$I_{\text{tot}} = \int_0^{\infty} dt \frac{\sigma I_0}{\tau_{\text{int}}} e^{-t/\tau_{\text{int}}} \frac{-\text{Li}_2\left(-2\pi^2 N_0^{\text{max}} R_{\text{int}}^3 \text{erf}\left(\sqrt{t/\tau_{\text{int}}}\right)/3\right)}{2\pi^2 N_0^{\text{max}} R_{\text{int}}^3 \text{erf}\left(\sqrt{t/\tau_{\text{int}}}\right)/3}.$$

Modeling the luminescence yield



$R_{\text{int}} = 3 \text{ nm}$

Main conclusion

The reason of nonlinear luminescence quenching and non-proportional response of the studied undoped and doped oxides and fluorides lies in the second order interaction – dipole-dipole interaction of excitons

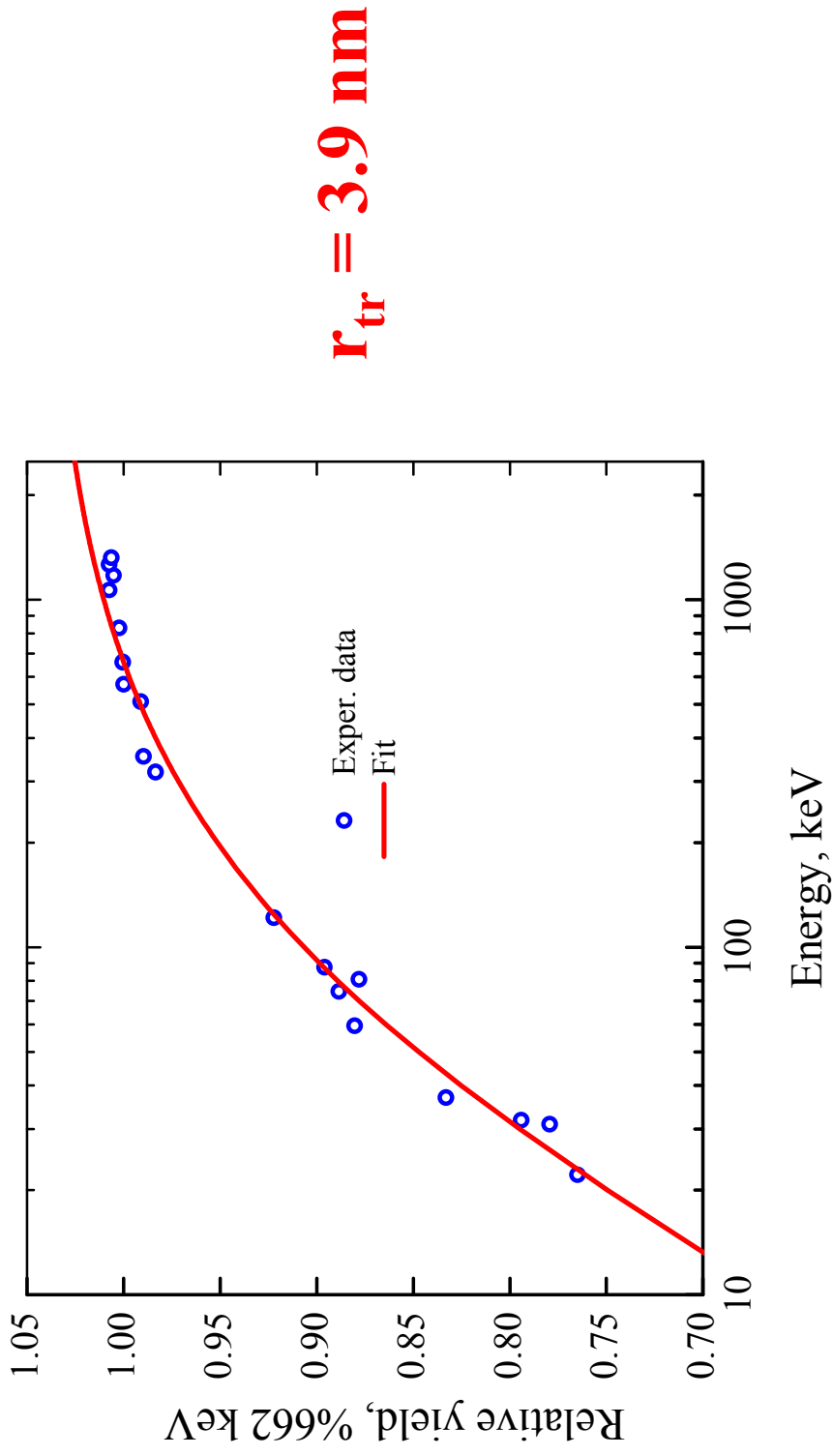
Modeling non-proportionality in terms of the dipole-dipole interaction radius

$$Y(E_0) = \frac{1}{E_0} \int_0^\infty \frac{\eta e^{-t/\tau}}{\tau E_{eh} a(t)} \int_0^{E_0} \frac{\ln \left[\frac{1 + a(t)b(x)}{b(x)} \right]}{b(x)} dx dt,$$

$$a(t) = \frac{2\pi\eta R_{d-d}^3}{3r^2 E_{eh}} \operatorname{erf} \left(\sqrt{t/\tau} \right)$$

$$b(E) = \frac{e^4 \rho_e}{8\pi\epsilon_0^2 E} \ln \left(1.164 \frac{E + 0.81I}{I} \right).$$

Non-proportionality of CdWO₄ defined as the light yield relative to that at 662 keV



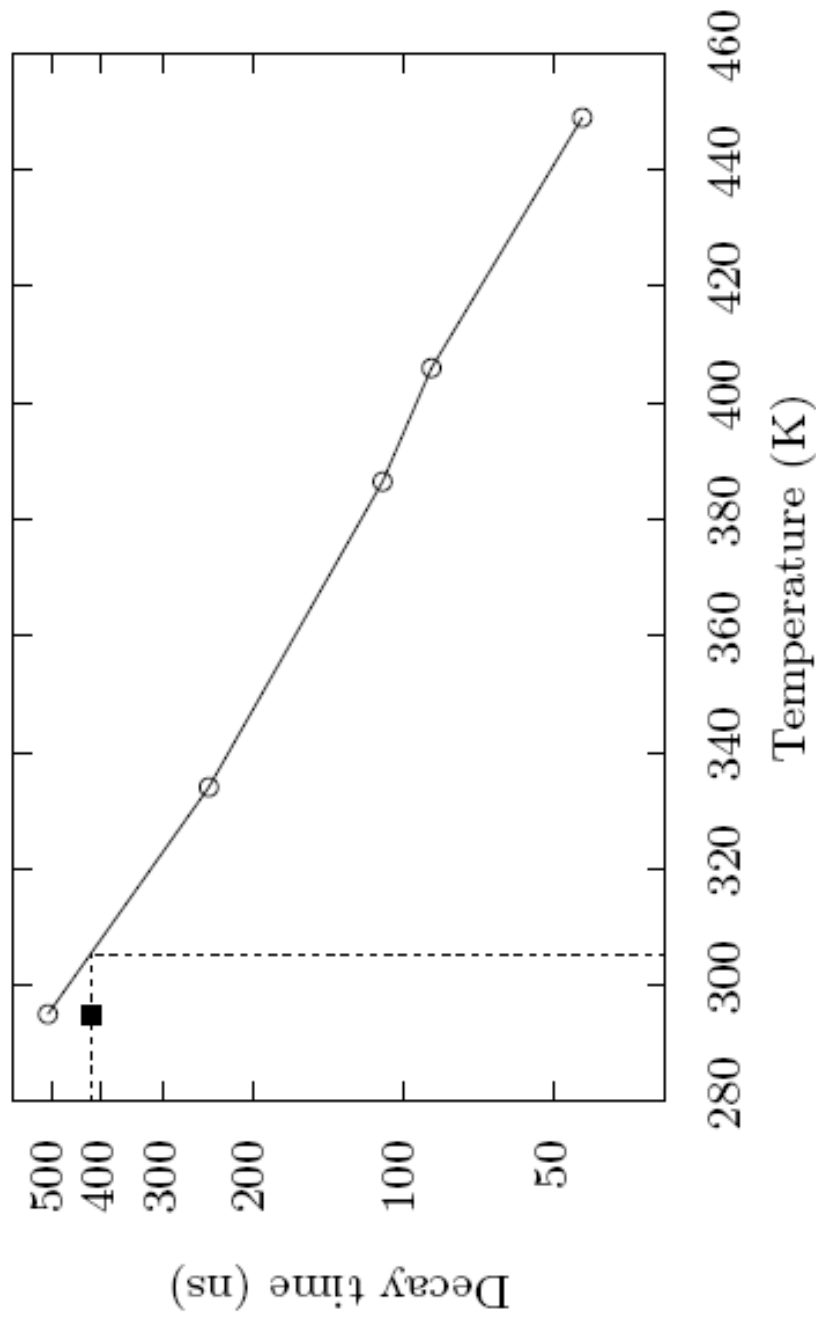
Exper. Data -- W. Klamra, T. Szczesniak, M. Moszynski, et al., J. Instrum. 7, P03011 (2012)

Conclusion

Modeling studies with UV/VUV pulsed excitation are useful for understanding scintillator non-proportionality problem

Thank you for your attention

Crystal heating with 100-fs pulses



Theoretical analysis

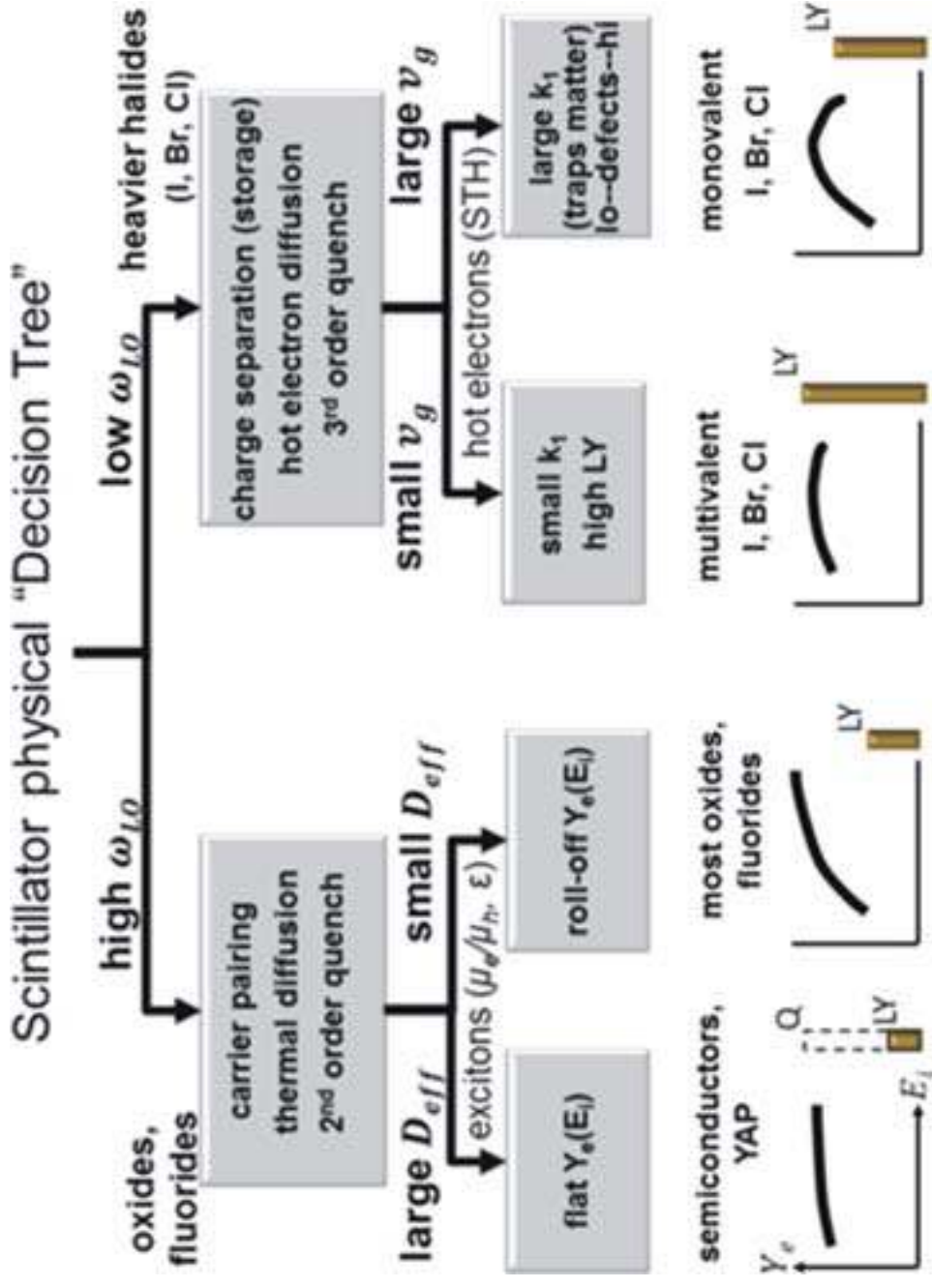
- A. N. Vasil'ev, IEEE Trans. Nucl. Sci. 55, 1054 (2008).
G. Bizarri et al., J. Appl. Phys. 105, 044507 (2009).
R. T. Williams et al., phys. stat. sol. (b) 248, 426 (2011).
W. W. Moses et al., IEEE Trans. Nucl. Sci. PP, 1 (2012).
Qi LI et al., J. Appl. Phys. 109, 123716 (2011)
Qi Li et al., P hys. Status Solidi RRL 6, No. 8, 346–348 (2012).

Main directions of studies

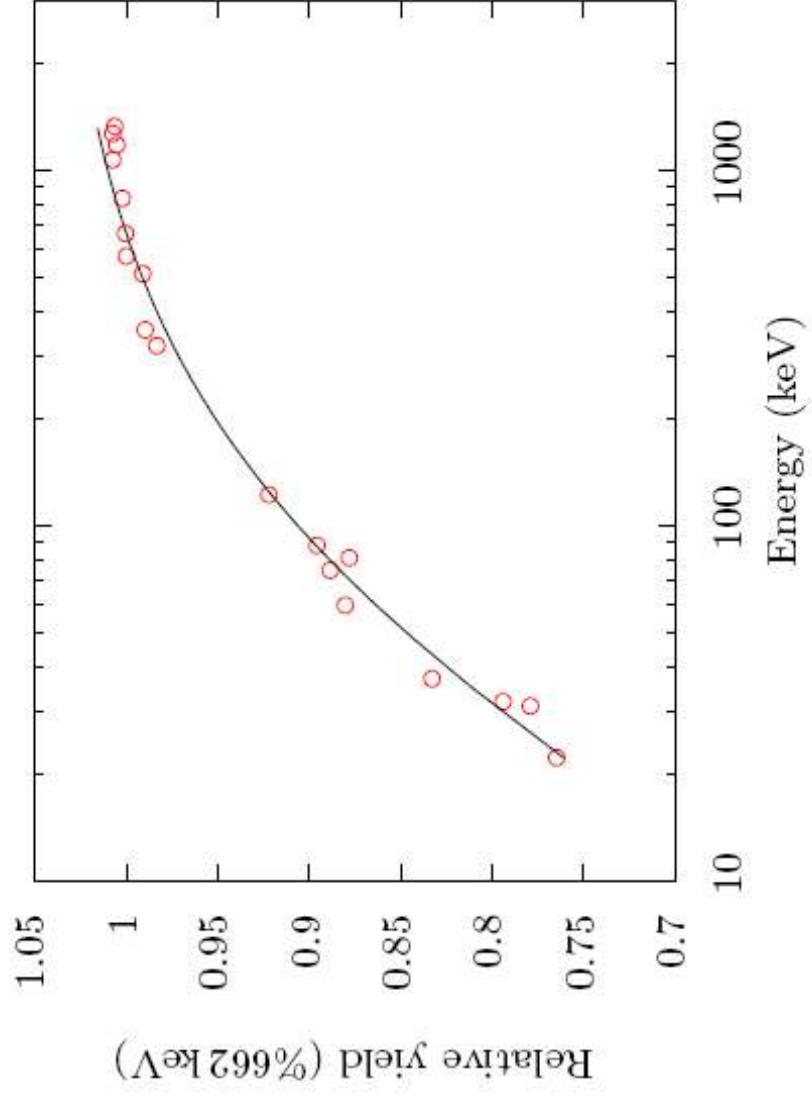
(factors that influence proportionality of LY):

1. Charge carrier thermalization rate and path
2. Diffusion of charge carriers and excitons:
 - average velocity of hot electrons
 - mobility of thermalized charge carriers
 - hole self-trapping
3. Quenching of luminescence
 - linear – trapping at defects and impurities
 - nonlinear – second order Förster, third order Auger

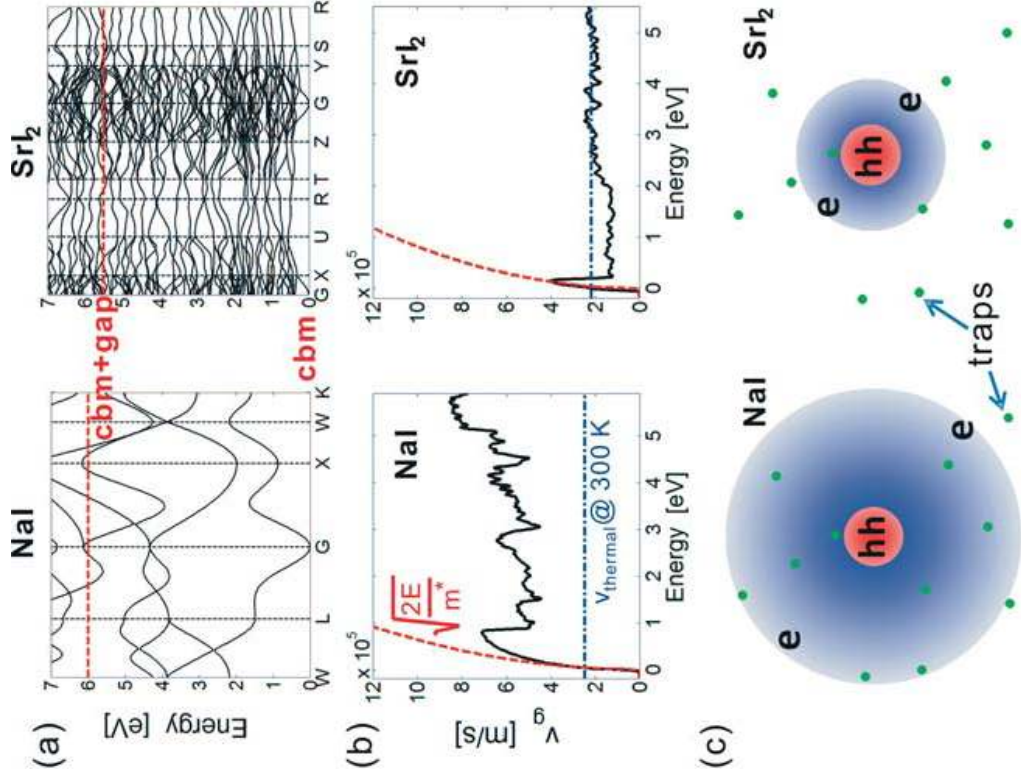
Nonproportionality in solids



Qi Li et al., Phys. Status Solidi RRL 6, No. 8, 346–348 (2012).



Group velocity of hot electrons



Qi Li et al., Phys. Status Solidi RRL **6**, No. 8, 346–348 (2012).

**Non-proportional response of scintillators
in visualization screens used in diagnostics of
intense fs photon beams in VUV**

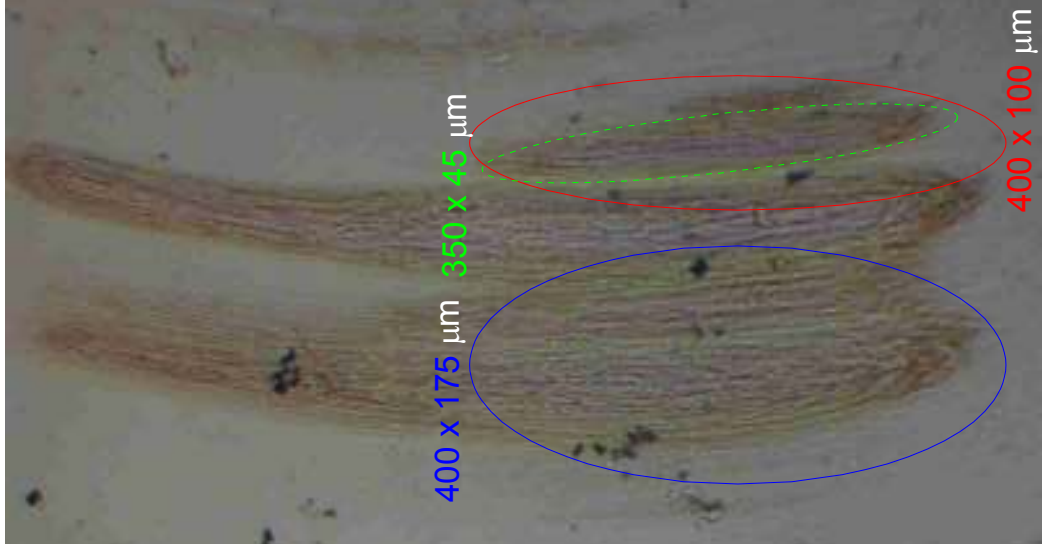
Free electron laser



FEL in VUV “FLASH” at DESY
260 m long laser
02/04/2009

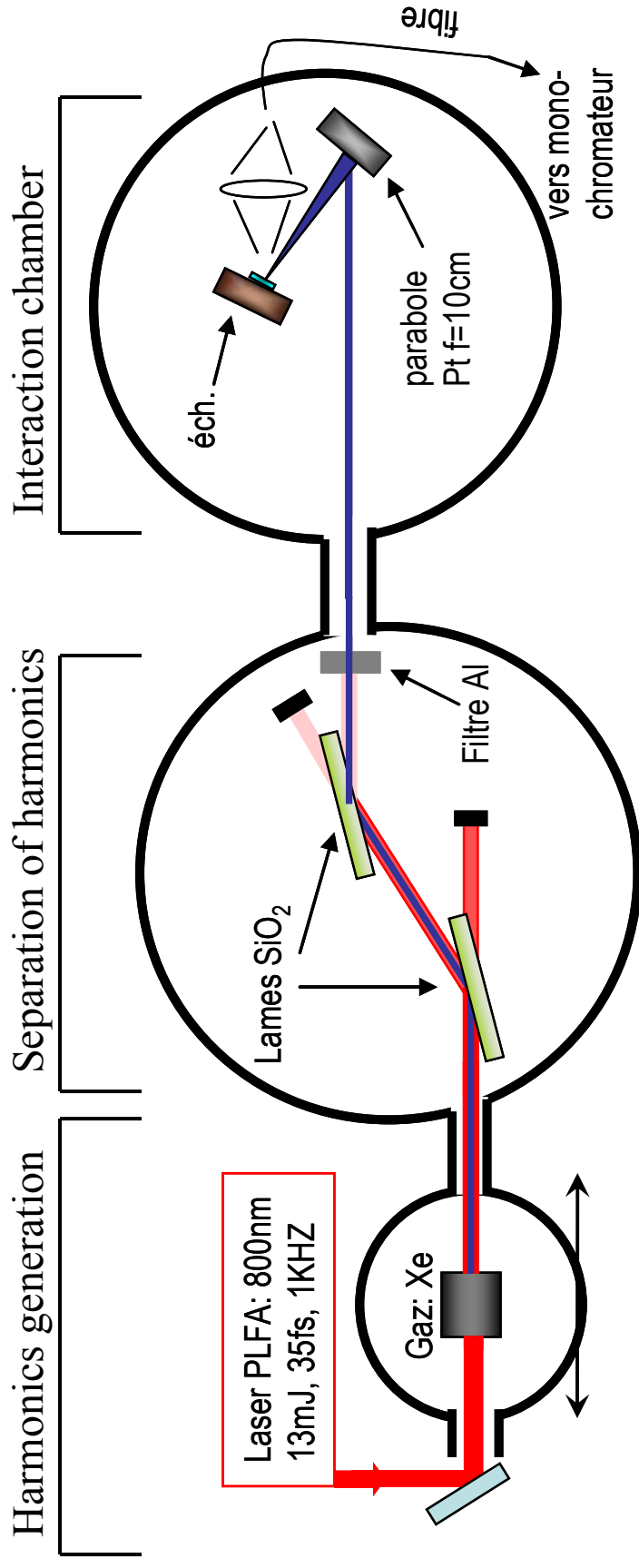
FLASH properties

25 fs pulses
30 μJ pulse energy
up to $2 \cdot 10^{12}$ photons
per pulse
 $\sim 10^{12}$ W/cm^2
Photon energy
up to 200 eV



- A comprehensive review of recent theoretical models:
Moses et al., IEEE Trans. Nucl. Sci. 59 (2012) 2038.
- A systematic review of experimental data on photon nonproportional response:
Khodyuk&Dorenbos, IEEE Trans. Nucl. Sci. 59 (2012) 3320

Experiment. High-density VUV excitation



~1 nJ, 15 fs

density of excitations in the VUV (20- 30 eV) > 10^{20} cm^{-3}

-Luminescence decay and spectra were measured

UV laser excitation of CaWO_4

