

# Linear and nonlinear effects in luminescence decay kinetics in wide- gap scintillating materials

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# Motivation

## Decay kinetics of CdWO<sub>4</sub> under different excitations

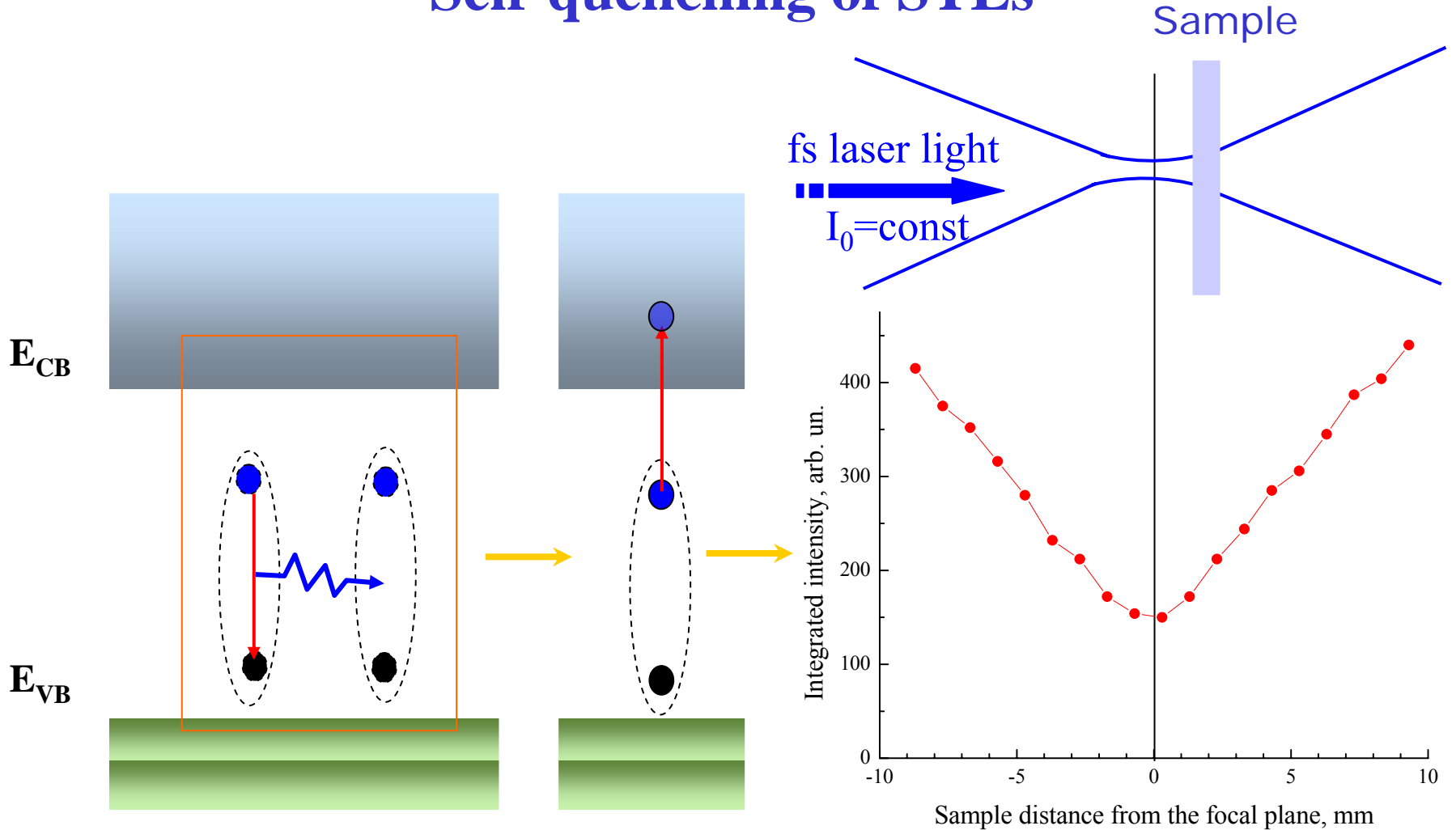
- 0.8  $\mu\text{S}$  Gillette, R.H., 1950. Rev. Sci. Instrum. 21, p. 294
- 1.1  $\mu\text{S}$ , 14.5  $\mu\text{S}$  D. Kinloch et al., IEEE Trans. Nucl. Sci. 41, 752 (1994).
- 2  $\mu\text{S}$  R. Deych et al., Proc. SCINT95, 1996, p. 36.
- 5  $\mu\text{S}$  C.L. Melcher et al., IEEE Trans. Nucl. Sci. 36, 1188 (1989)
- 7.8  $\mu\text{S}$  Beard, G.B. et al., 1962. J Appl. Phys.. 33, p. 144
- 9  $\mu\text{S}$  B.C. Grabmaier. IEEE Trans. Nucl. Sci. 31, 372 (1984)
- 13-15  $\mu\text{S}$  under optical excitation! Many papers.

### Central idea:

The differences observed in the decay kinetics are due to the different densities of electronic excitations created in tracks of x-ray or  $\gamma$  quanta of different energies used in the studies of scintillation response. (?)

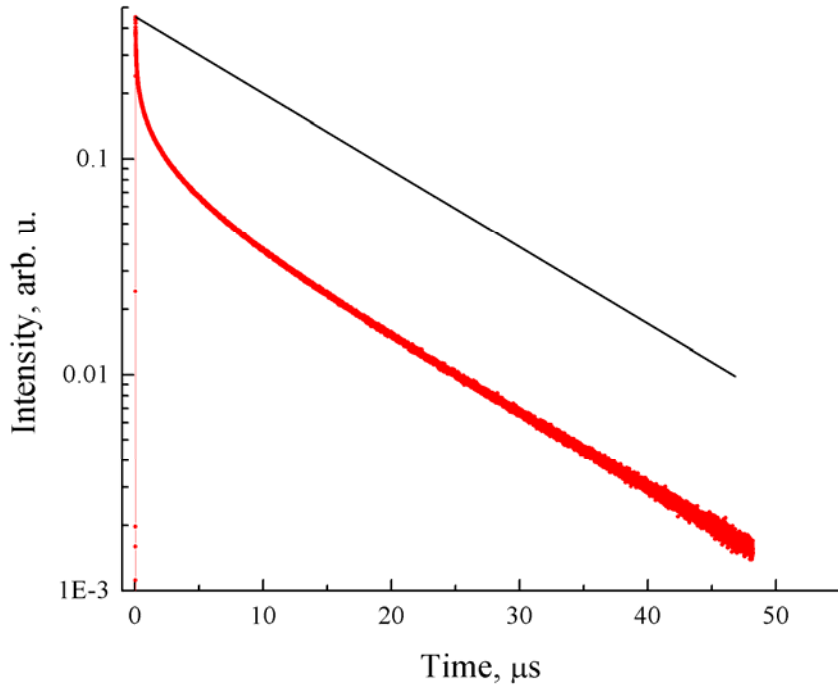
# Frenkel excitons created at high densities.

## Self-quenching of STEs

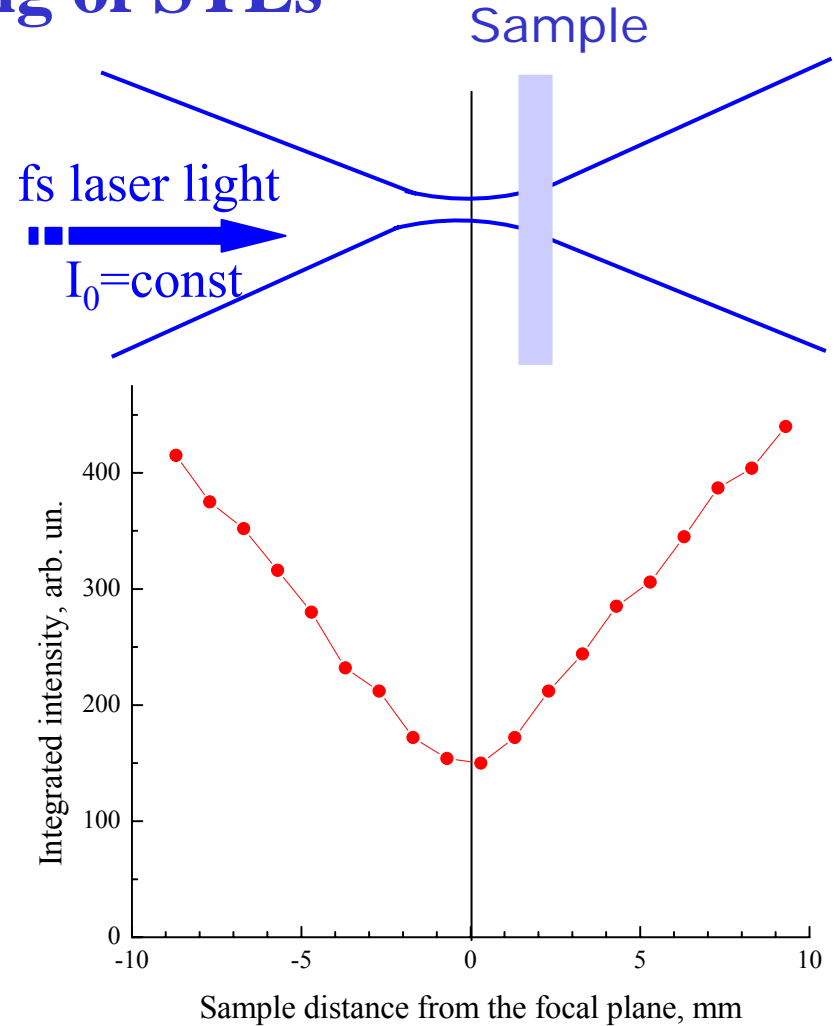


$\text{CaWO}_4$ ,  $E_{\text{exc}} = 5$  eV (247.5 nm), 80 fs pulse,  
1  $\mu\text{J}$  pulse energy, 70  $\mu\text{m}$  beam waist

# Frenkel excitons created at high densities. Self-quenching of STEs

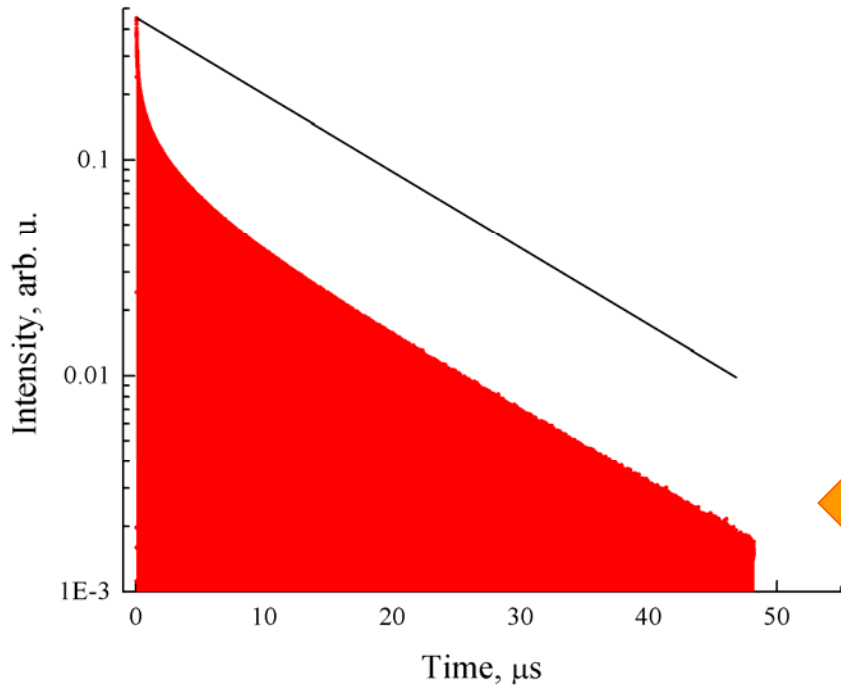


CdWO<sub>4</sub>,  $E_{\text{exc}}=4.84$  eV (256.4 nm),  
80 fs pulse, 0.6 μJ pulse energy,  
130 μm beam waist

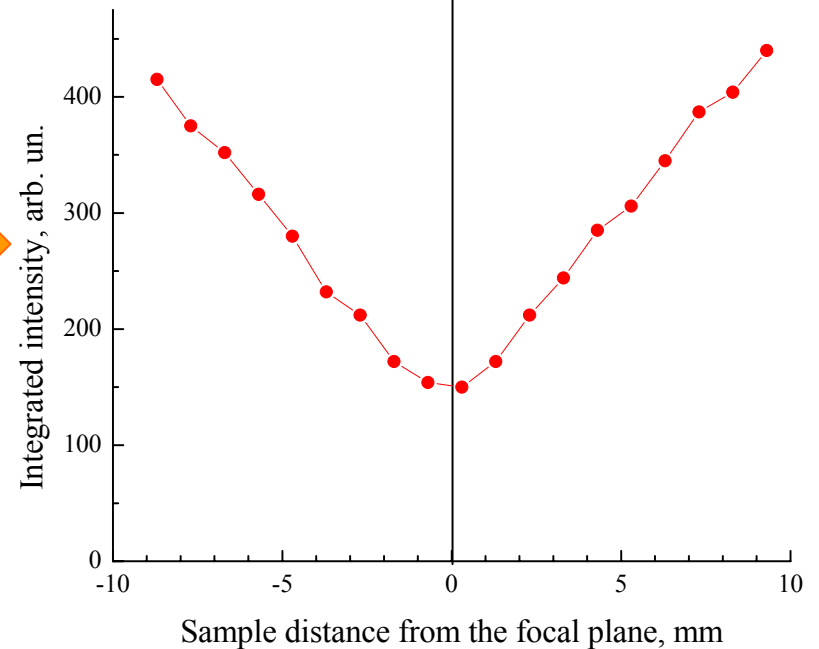
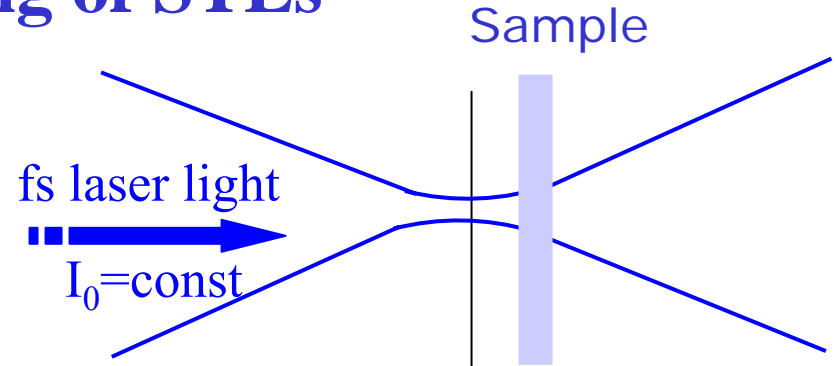


CaWO<sub>4</sub>,  $E_{\text{exc}}=5$  eV (247.5 nm), 80 fs pulse,  
1 μJ pulse energy, 70 μm beam waist

# Frenkel excitons created at high densities. Self-quenching of STEs



$\text{CdWO}_4$ ,  $E_{\text{exc}} = 4.84 \text{ eV}$  (256.4 nm),  
80 fs pulse, 0.6 μJ pulse energy,  
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$\text{CaWO}_4$ ,  $E_{\text{exc}} = 5 \text{ eV}$  (247.5 nm), 80 fs pulse,  
1 μJ pulse energy, 70 μm beam waist

# Förster dipole-dipole energy transfer

M. Kirm et al, Phys. Rev. B **79** (2009) 233103

•Exciton concentration: 
$$\frac{\partial n(\mathbf{r}, t)}{\partial t} = -\frac{n(\mathbf{r}, t)}{\tau_r} - \gamma_{d-d}(t, \mathbf{r})n^2(\mathbf{r}, t)$$

•Dipole-dipole energy transfer rate: 
$$\sim \frac{1}{\tau_r} (R_{d-d} / R)^6$$

•Dipole-dipole transfer radius: 
$$R_{d-d}^6 \propto \int \omega^{-4} F_{em}(\omega) F_{exc}(\omega) d\omega$$

$$I(t) = \frac{\sigma I_0}{\tau} e^{-t/\tau} \frac{-Li_2\left(-\frac{2}{3}\pi^2 R_{d-d}^3 N_{\max} \operatorname{erf}\left(\sqrt{t\tau^{-1}}\right)\right)}{\frac{2}{3}\pi^2 R_{d-d}^3 N_{\max} \operatorname{erf}\left(\sqrt{t\tau^{-1}}\right)}$$

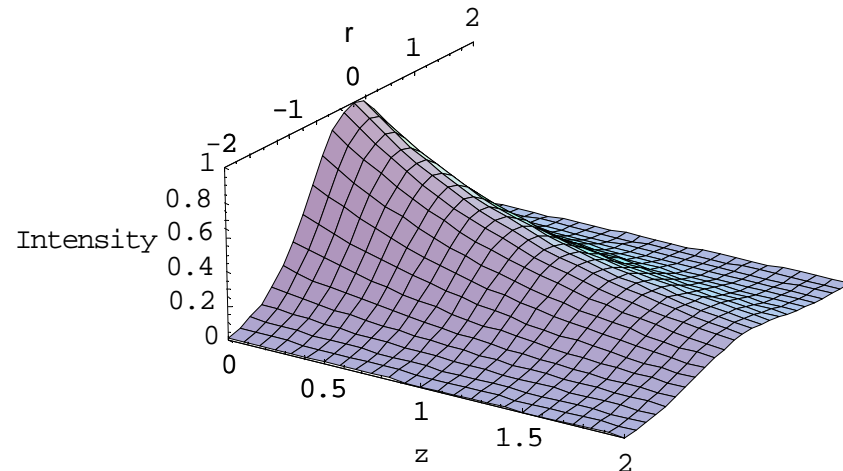
$$N_{\max} \equiv I_0 \frac{\sigma\alpha}{\pi a^2}$$

$I_0$  – number of photons in a pulse

$\alpha$  – absorption coefficient

$\sigma$  – exciton yield

$a$  – pulse radius



# Experiments performed

- High-order harmonics generation (HHG): 23-32 eV, 10-15 fs

**M. Kirm *et. al.*, Phys. Rev. B 79, 233103 (2009)**

- Free electron laser (FEL): 89 eV, 25 fs

**S. Vielhauer *et. al.*, Phys. Sol. State, 50, 1789 (2008)**

Optical parametric amplifier (OPA, 240 - 2600 nm, 1-200  $\mu$ J/pulse, 100 fs,

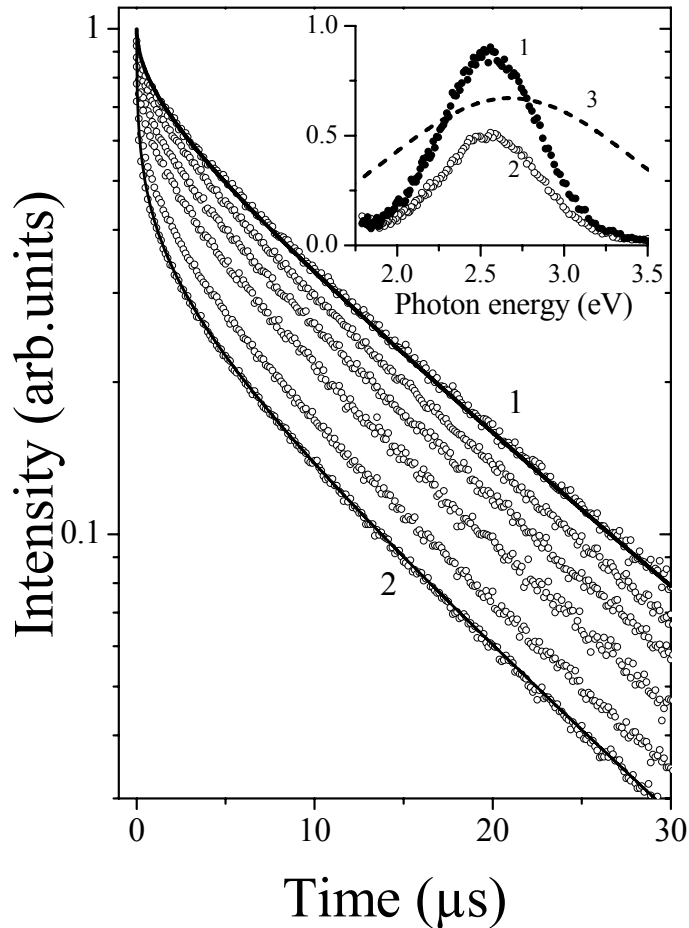
1 kHz (Laser Research Centre, Vilnius University)

**V. Nagirnyi *et. al.*, IEEE Trans. Nucl. Sci. 57, 1182 (2010)**

**R. Laasner *et al.*, under preparation.**

# Estimation of parameters

(High order harmonic generation, Saclay)



$$N_0^{\max} = I_0 \frac{\alpha \sigma}{\pi a^2}$$

- $\alpha$  was taken  $10^5 \text{ cm}^{-1}$  for photon energy 23-32 eV, 15 fs

- $\sigma = 2 - 3$  for 23-32 eV



- $a$  measured  $70 \text{ μm}$

- $N_0^{\max} = 2.5 \times 10^{20} \text{ cm}^{-3}$

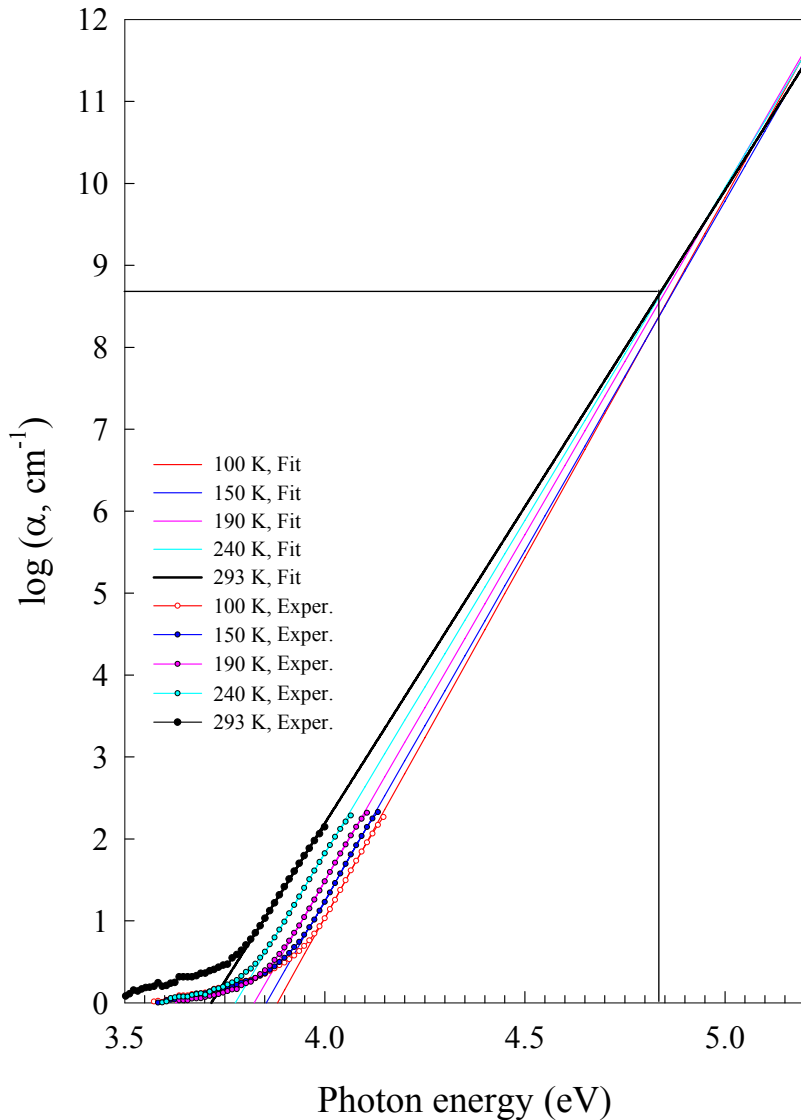
- $R_{d-d} = 2.1 \text{ nm}$

Lattice parameters:

$a = 5.029 \text{ Å}, b = 5.859 \text{ Å}, c = 5.074 \text{ Å}$



# Estimation of parameters 2

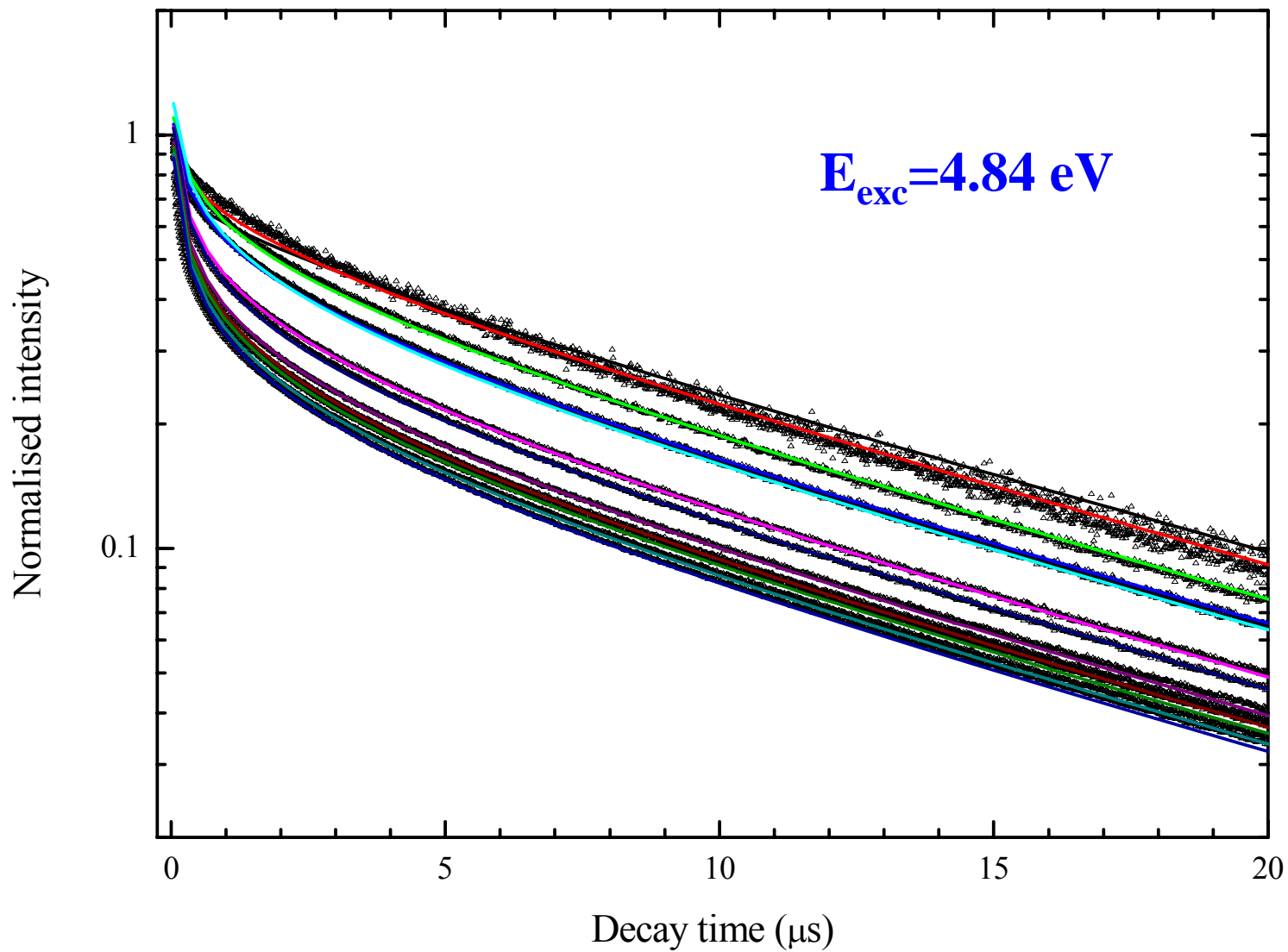


$$N_0^{\max} = I_0 \frac{\alpha \sigma}{\pi a^2}$$

$E_{\text{exc}} = 4.84 \text{ eV}, 100 \text{ fs}$

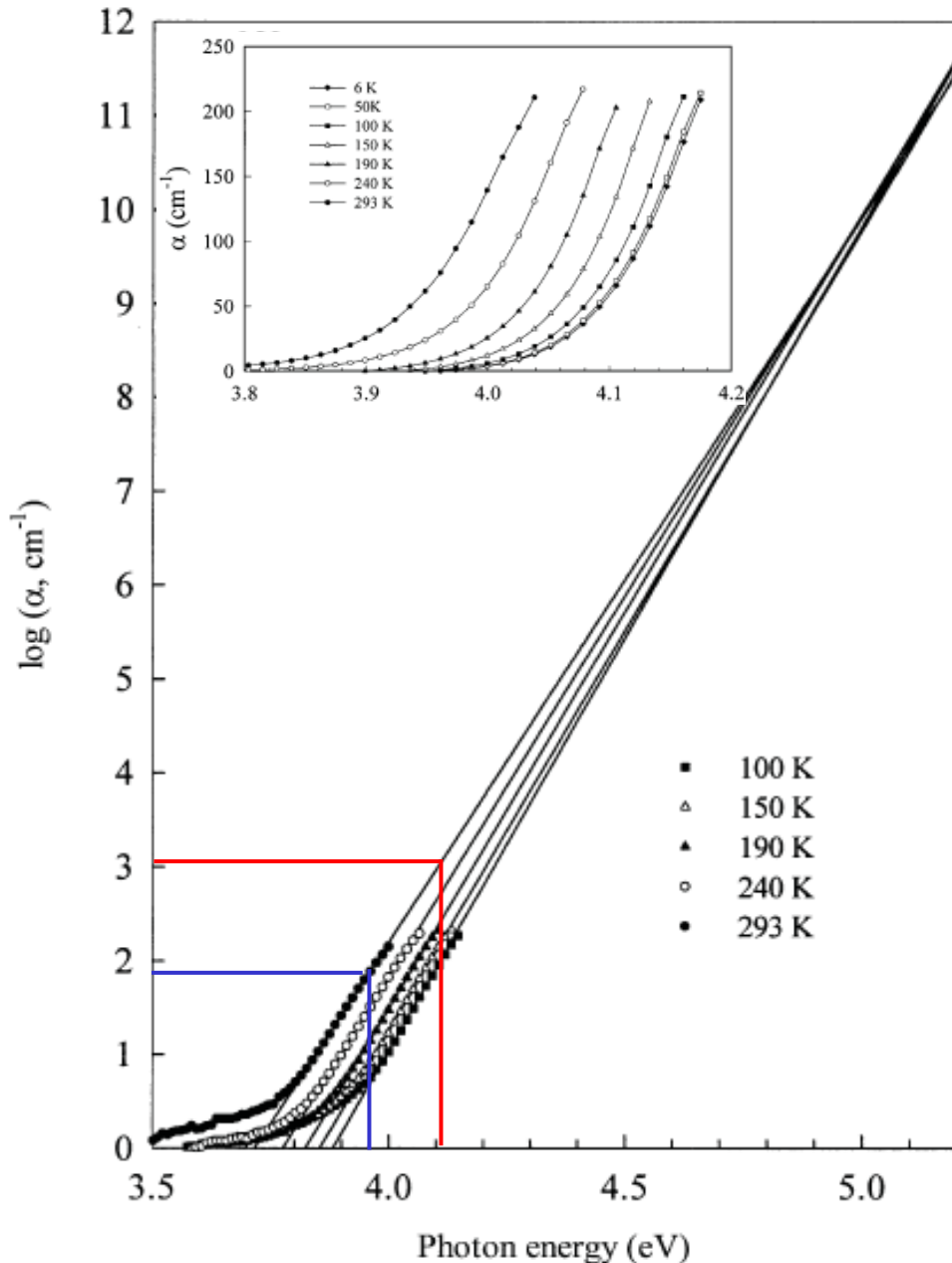
- $\sigma = 1$
- $a$  measured  $60 \mu\text{m}$
- $\alpha = 10^6 \text{ cm}^{-1}$  ← ?
- $R_{d-d} = 3 \text{ nm}$
- $N_0^{\max} = 6 \times 10^{21} \text{ cm}^{-3}$

# Fitted curves for CdWO<sub>4</sub>



# CdWO<sub>4</sub> excitation in the Urbach tail region

V. Nagirnyi et al., J. Lumin. **102**, 597 (2003)



313 nm (3.96 eV)

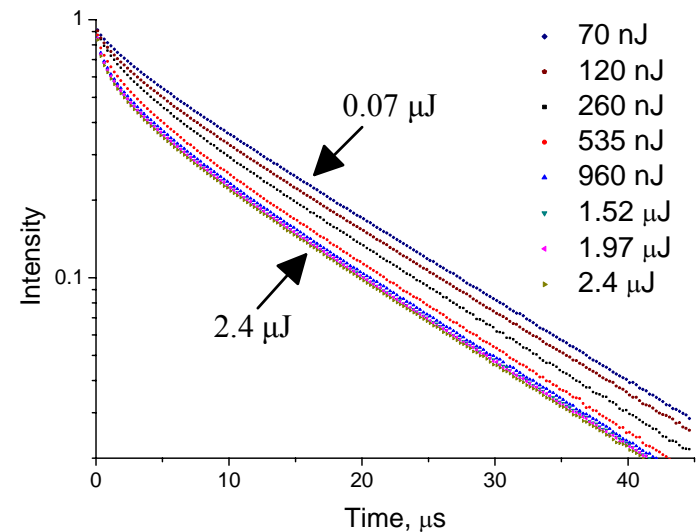
•  $\alpha = 77.6 \text{ cm}^{-1}$

•  $\sigma = 1$

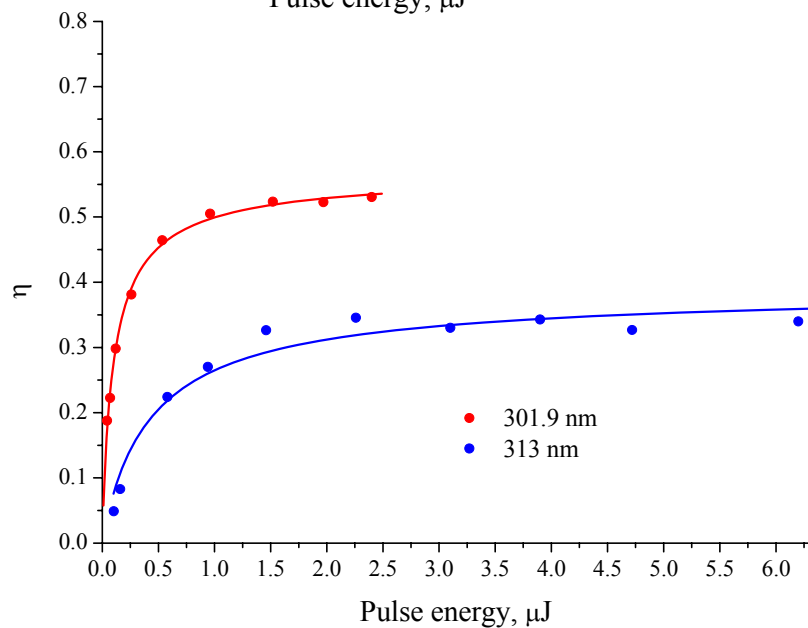
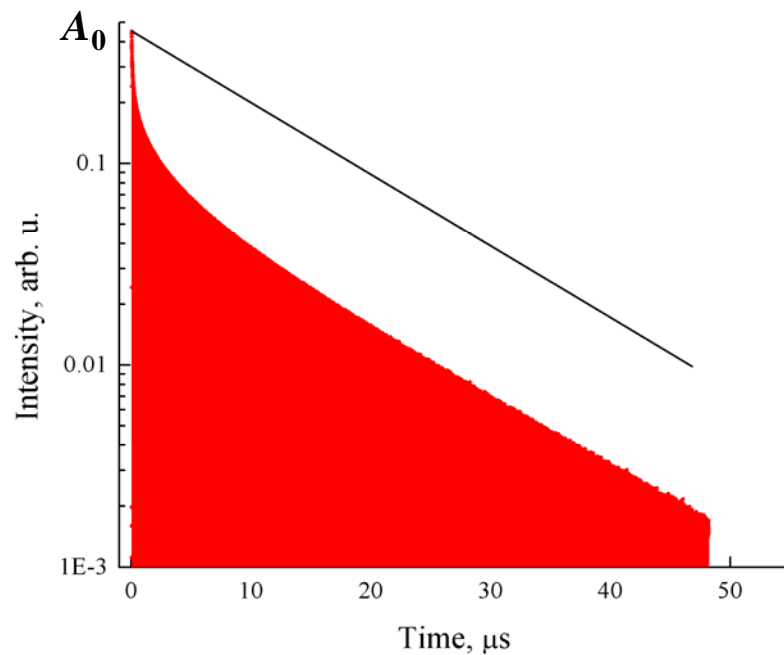
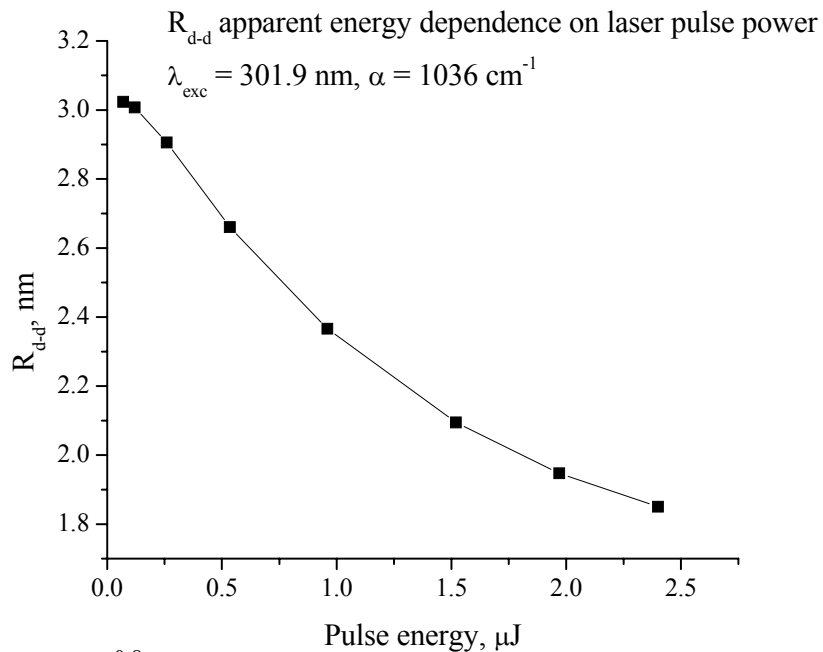
301.9 nm (4.11 eV)



•  $\alpha = 1036 \text{ cm}^{-1}$

•  $\sigma = 1$

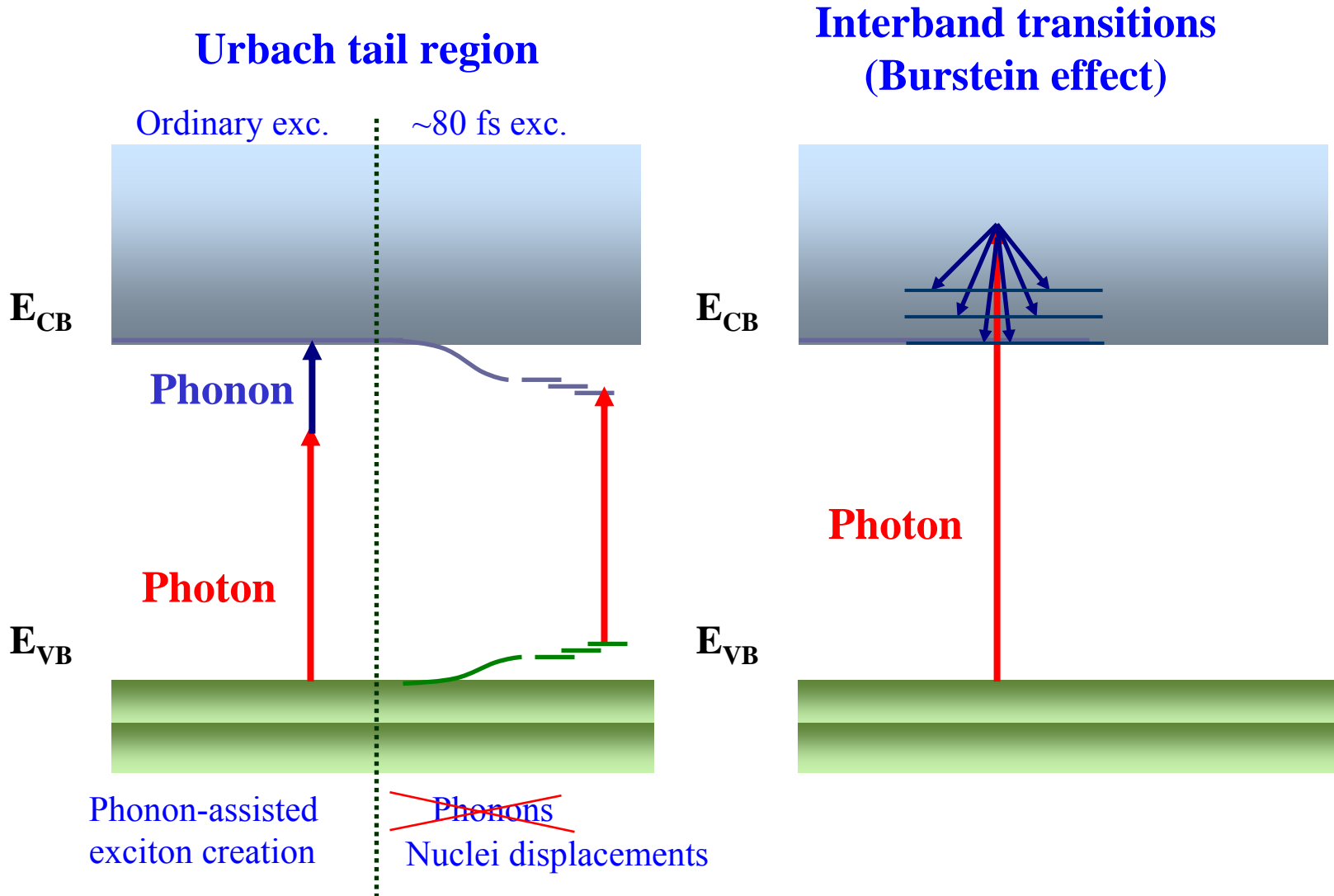


# Problem




$$\eta = 1 - \frac{\int I_{\text{exp}}(t) dt}{A_0 \tau_r}$$


# Reasons of the saturation of excitonic absorption



# Modeling

80 fs pulses



Saturated absorption



$$\alpha = \alpha_{lin} \left( 1 - n(\mathbf{r}, t) / n_0 \right)$$

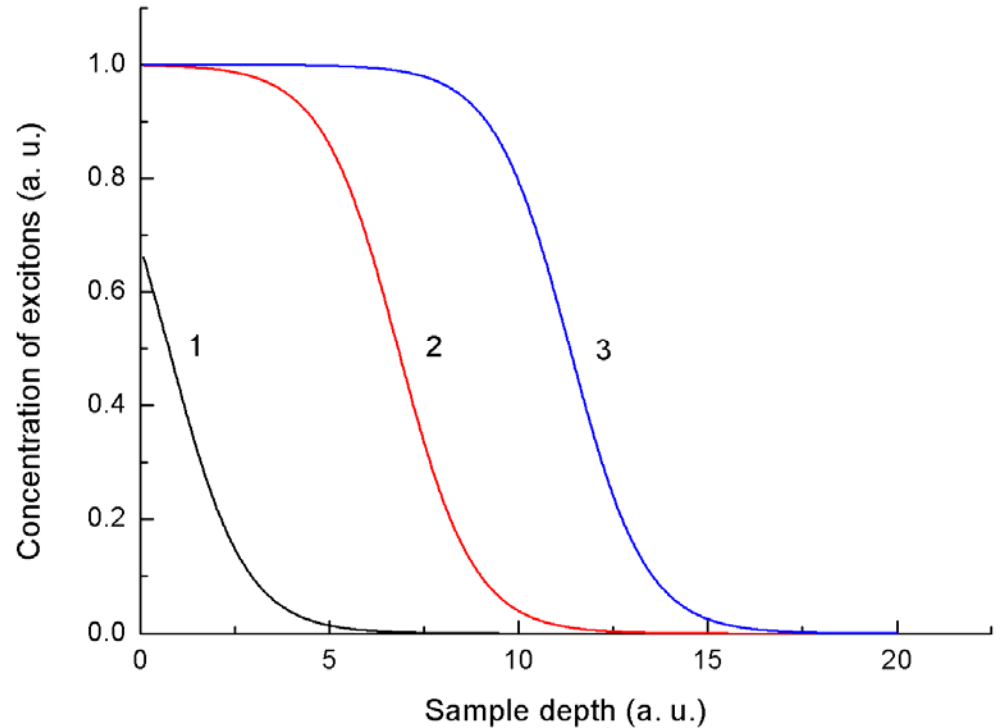
$n_0$  – maximum possible concentration of excitations



$$I(t) = \frac{\pi a^2 n_0}{\tau \alpha} e^{-t/\tau} \int_0^{\infty} \frac{\frac{I_0 \alpha}{\pi a^2 n_0} \ln \left( e^x + (e^x - 1) \frac{2}{3} \pi^2 R_{d-d}^3 n_0 \operatorname{erf}(\sqrt{t\tau^{-1}}) \right)}{x \left( 1 + \frac{2}{3} \pi^2 R_{d-d}^3 n_0 \operatorname{erf}(\sqrt{t\tau^{-1}}) \right)} dx$$



302 nm :  $R_{d-d} = 3.7$  nm  
 $n_0 = 5.4 \times 10^{18}$  cm<sup>-3</sup>



**$R_{d-d} = 3.7$  nm**

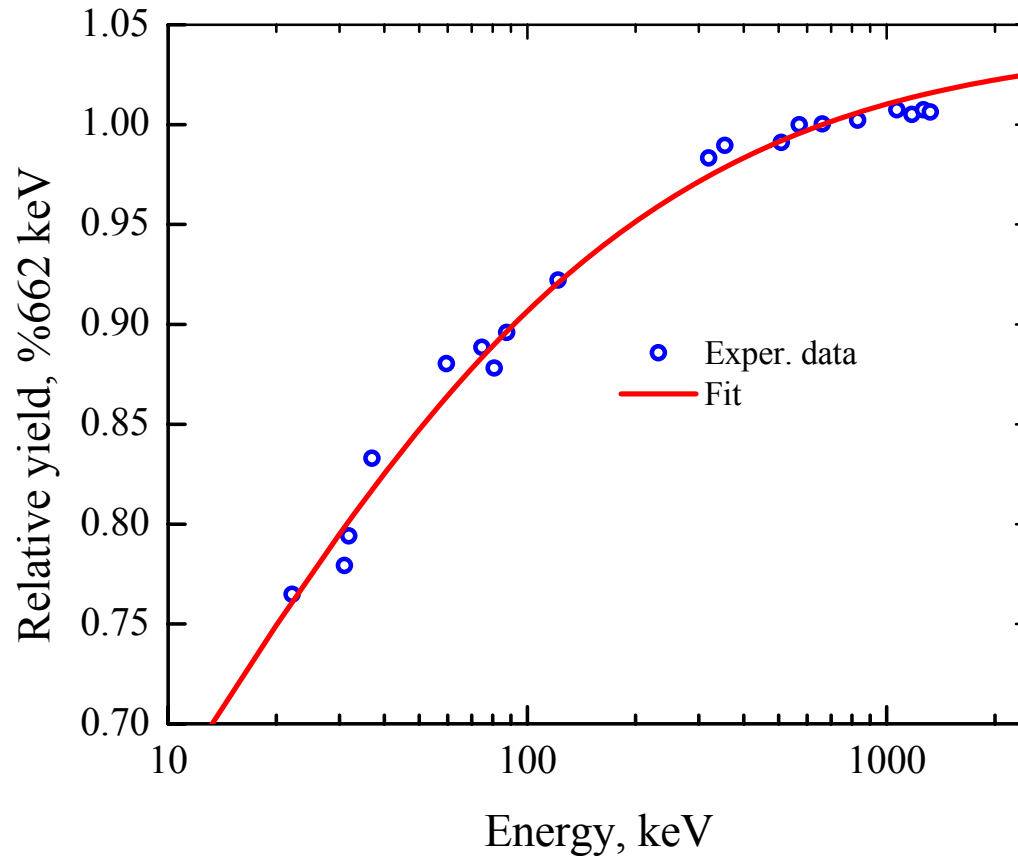
# Modeling non-proportionality in terms of the Förster radius

$$Y(E_0) = \frac{1}{E_0} \int_0^\infty \frac{\eta e^{-t/\tau}}{\tau E_{eh} a(t)} \int_0^{E_0} \frac{\ln[1 + a(t)b(x)]}{b(x)} dx dt,$$

$$a(t) = \frac{2\pi\eta R_{d-d}^3}{3r^2 E_{eh}} \operatorname{erf}\left(\sqrt{t/\tau}\right)$$

$$b(E) = \frac{e^4 \rho_e}{8\pi\epsilon_0^2 E} \ln\left(1.164 \frac{E + 0.81I}{I}\right).$$

# Non-proportionality of $\text{CdWO}_4$ defined as the light yield relative to 662 keV.



$$r_{\text{tr}} = 3.9 \text{ nm}$$

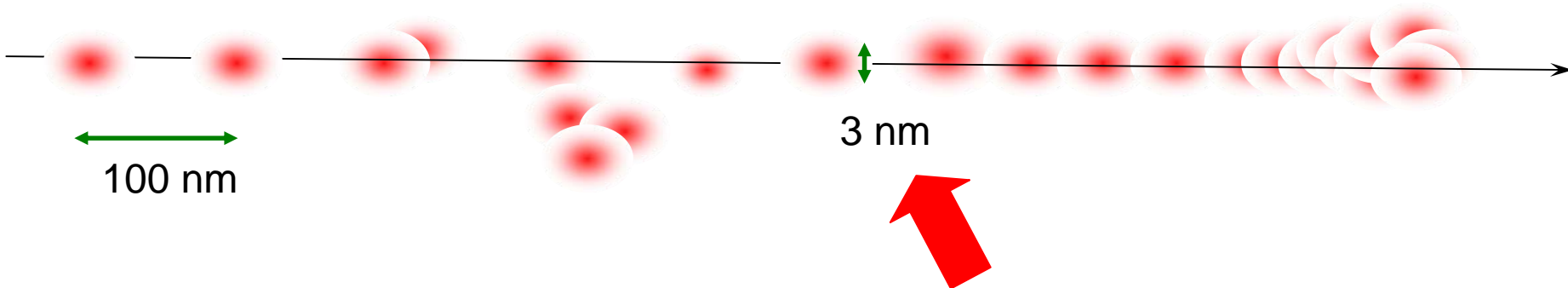
Exper. Data -- W. Klamra, T. Szczesniak, M. Moszynski, et al., J. Instrum. **7**, P03011 (2012)



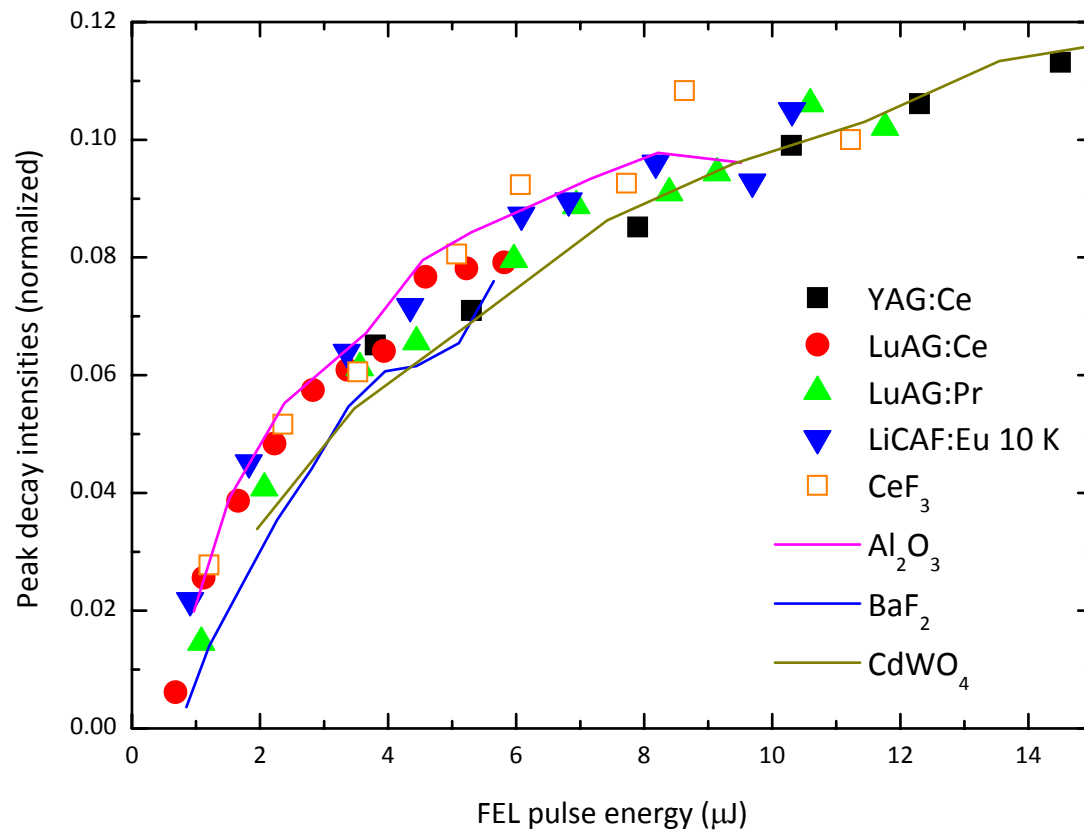
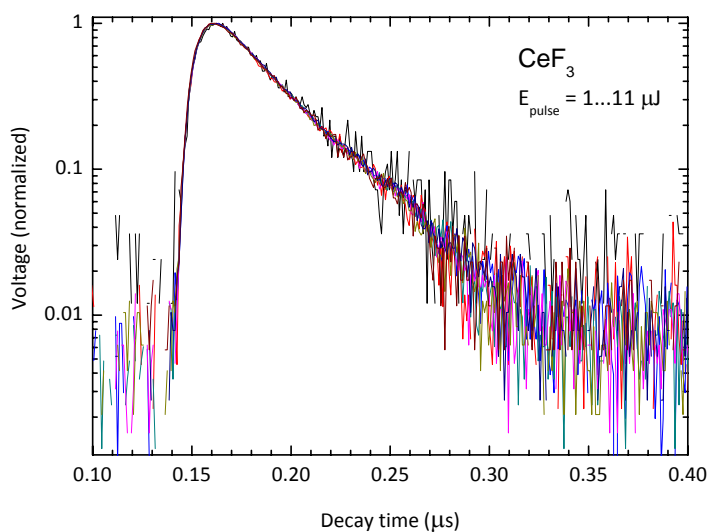
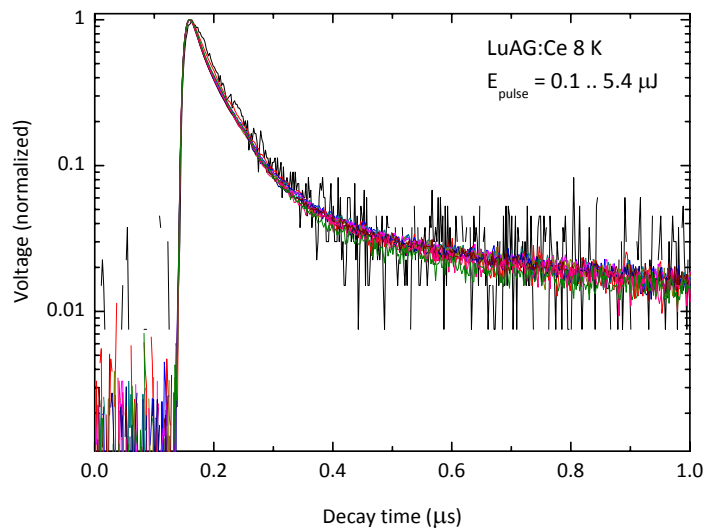
# Track spatial and temporal structure

(A.N. Vasil'ev, SCINT'2009)

Initial electron track structure is defined by isolated and overlapped clusters of excitations with initial size of about 3 nm (just after initial recombination and thermalization of electrons and holes, ps time domain) and distances between clusters are about 1 to 100 nm.



# RE activated scintillators



# Theoretical analysis, further works

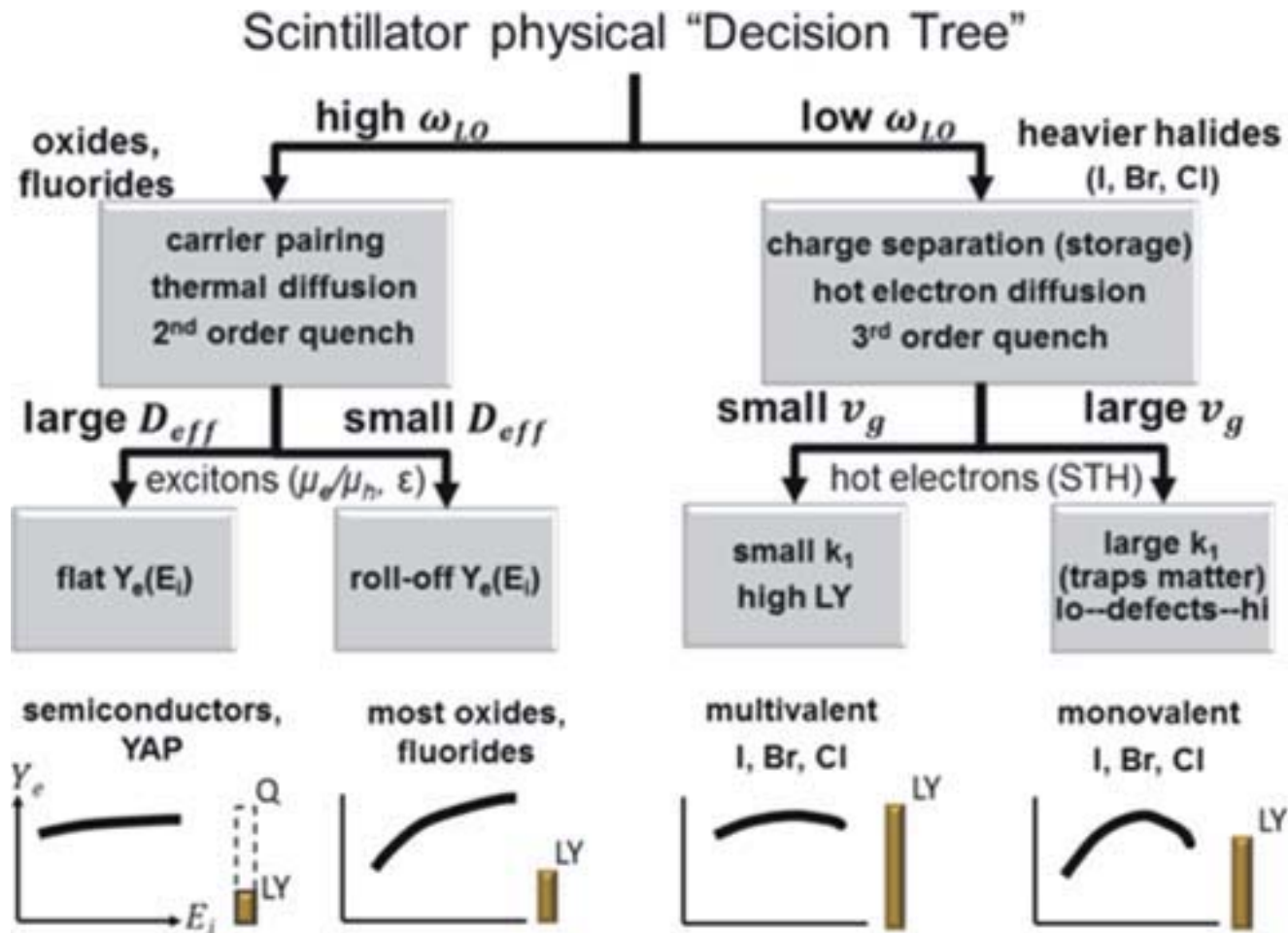
- A. N. Vasil'ev, IEEE Trans. Nucl. Sci. 55, 1054 (2008).  
G. Bizarri et al., J. Appl. Phys. 105, 044507 (2009).  
G. Bizarri et al., J. Lumin. 129, 1790 (2009).  
R. T. Williams et al., phys. stat. sol. (b) 248, 426 (2011).  
W. W. Moses et al., IEEE Trans. Nucl. Sci. PP, 1 (2012).  
Qi LI et al., J. Appl. Phys. 109, 123716 (2011)  
Qi Li et al., Phys. Status Solidi RRL 6, No. 8, 346–348 (2012).

## Main directions of studies

### (factors that influence proportionality of LY):

1. Charge carrier thermalization rate
2. Diffusion of charge carriers and excitons:
  - group velocity of hot electrons
  - mobility of thermalized charge carriers
  - hole self-trapping
3. Quenching of luminescence
  - linear – trapping at defects and impurities
  - nonlinear – second order Förster, third order Auger

# Nonproportionality in solids



Qi Li et al., Phys. Status Solidi RRL 6, No. 8, 346–348 (2012).

## To study

- Charge carrier relaxation (exciton formation)
- Charge carrier mobility (diffusion)
- Mutual interaction of electronic excitations
- Interaction of electronic excitations with impurities and defects, charge trapping

## Two additional experiments

- High-density excitation; the study of interaction of electronic excitations (Saclay, Vilnius)
- Time-resolved interferometry; the study of thermalization and trapping dynamics of electronic excitations (Saclay)

**Thank you for attention**